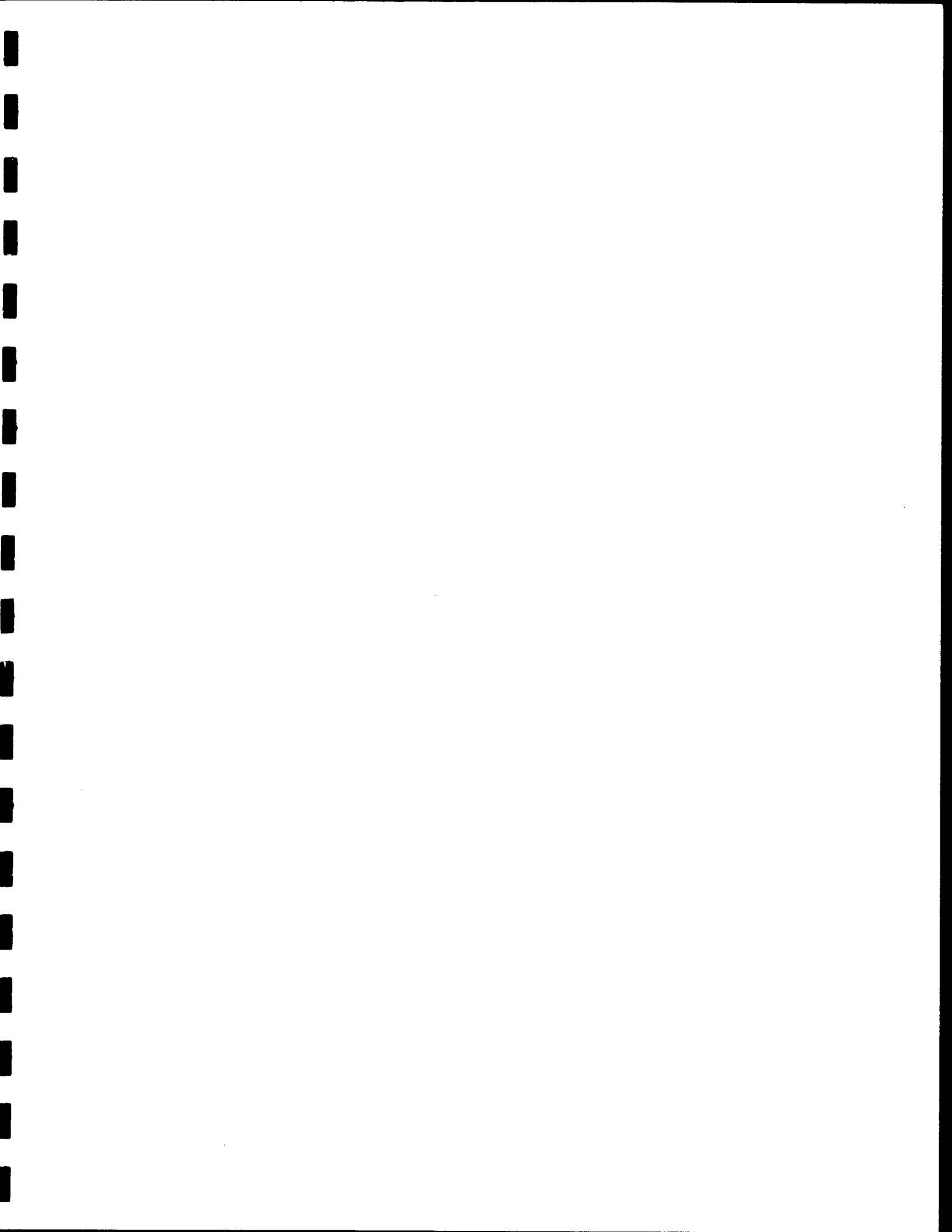


Haskell Workshop
Sponsored by ACM SIGPLAN
Held in conjunction with ICFP97
Amsterdam
Saturday, June 7, 1997



Haskell Workshop

Sponsored by ACM SIGPLAN and held in conjunction with ICFP97, Amsterdam, Saturday, June 7, 1997

The definition of Haskell 1.4 has recently been released, but it is clear that there are many exciting opportunities ahead for developing and enhancing the language. Some of these will be in direct response to needs demonstrated by large-scale applications written in Haskell, or by Haskell being used in novel and interesting ways. Other developments will be driven by more theoretical considerations, whether they are moving in the direction of increased expressibility or, alternatively, simplifications to the language by recognizing unifying concepts. The purpose of the workshop is to provide a forum where possible future development directions for Haskell may be discussed.

The program committee consisted of

- Lennart Augustsson (Chalmers)
- Mark Jones (Nottingham)
- John Launchbury (OGI) - Chair
- Erik Meijer (Utrecht)
- John Peterson (Yale)
- Satnam Singh (Glasgow)
- Peter Thiemann (Tuebingen)

and I thank them for their work in reviewing and selecting the papers. I also thank the organizers of ICFP97 for taking care of the local arrangements.

J. Launchbury
May 1997

Workshop Program

Session 1. Chair: Lennart Augustsson

9:00-9:30. *Type Classes: an exploration of the design space.* Simon Peyton Jones, Mark Jones, and Erik Meijer

9:30-10:00. *Polymorphic Extensible Records for Haskell.* Benedict R. Gaster

10:00-10:30. *The Design and Implementation of Mondrian.* Erik Meijer and Koen Claessen

10:30-11:00. BREAK

Session 2. Chair: John Peterson

11:00-11:30. *Reactive Objects in a Functional Language.* Johan Nordlander and Magnus Carlsson

11:30-12:00. *Debugging Reactive Systems in Haskell.* Amr Sabry and Jan Sparrud

12:00-12:30. *Bulk Types with Class.* Simon Peyton Jones

12:30-2:00. LUNCH

Session 3. Chair: Peter Thiemann

2:00-2:30. *Disposable Memo Functions.* Byron Cook and John Launchbury

2:30-3:00. *Green Card: a foreign language interface for Haskell.* Simon Peyton Jones, Thomas Nordin, and Alastair Reid

3:00-3:30. *Heap Compression and Binary I/O in Haskell.* Malcolm Wallace and Colin Runciman

3:30-4:00. BREAK

Session 4. Chair: John Launchbury

4:00-5:30. *Open-mike Session: What next for Haskell?* Participants are invited to make 5-minute statements on the future development of Haskell. These will be grouped by topic, and while the statements are limited to five minutes, any ensuing discussion is not. Anyone who wants to make a statement should indicate their desire in advance of the session.

Type classes: an exploration of the design space

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Mark Jones
University of Nottingham

Erik Meijer
University of Utrecht and Oregon Graduate Institute

May 2, 1997

Abstract

When type classes were first introduced in Haskell they were regarded as a fairly experimental language feature, and therefore warranted a fairly conservative design. Since that time, practical experience has convinced many programmers of the benefits and convenience of type classes. However, on occasion, these same programmers have discovered examples where seemingly natural applications for type class overloading are prevented by the restrictions imposed by the Haskell design.

It is possible to extend the type class mechanism of Haskell in various ways to overcome these limitations, but such proposals must be designed with great care. For example, several different extensions have been implemented in Gofer. Some of these, particularly the support for multi-parameter classes, have proved to be very useful, but interactions between other aspects of the design have resulted in a type system that is both unsound and undecidable. Another illustration is the introduction of constructor classes in Haskell 1.3, which came without the proper generalization of the notation of a context. As a consequence, certain quite reasonable programs are not typable.

In this paper we review the rationale behind the design of Haskell's class system, we identify some of the weaknesses in the current situation, and we explain the choices that we face in attempting to remove them.

1 Introduction

Type classes are one of the most distinctive features of Haskell (Hudak et al. [1992]). They have been used for an impressive variety of applications, and Haskell 1.3¹ significantly extended their expressiveness by introducing *constructor classes* (Jones [1993a]).

All programmers want more than they are given, and many people have bumped up against the limitations of Haskell's class system. Another language, Gofer (Jones [1994]), that has developed in parallel with Haskell, enjoys a much more liberal and expressive class system. This expressiveness is definitely both useful and used, and transferring from Gofer

¹The current iteration of the Haskell language is Haskell 1.4, but it is identical to Haskell 1.3 in all respects relevant to this paper.

to Haskell can be a painful experience. One feature that is particularly often missed is *multi-parameter type classes* — Section 2 explains why.

The obvious question is whether there is an upward-compatible way to extend Haskell's class system to enjoy some or all of the expressiveness that Gofer provides, and perhaps some more besides. The main body of this paper explores this question in detail. It turns out that there are a number of interlocking design decisions to be made. Gofer and Haskell each embody a particular set, but it is very useful to tease them out independently, and see how they interact. Our goal is to explore the design space as clearly as possible, laying out the choices that must be made, and the factors that affect them, rather than prescribing a particular solution (Section 4). We find that the design space is rather large; we identify nine separate design decisions, each of which has two or more possible choices, though not all combinations of choices make sense. In the end, however, we do offer our own opinion about a sensible set of choices (Section 6).

A new language feature is only justifiable if it results in a simplification or unification of the original language design, or if the extra expressiveness is truly useful in practice. One contribution of this paper is to collect together a fairly large set of examples that motivate various extensions to Haskell's type classes.

2 Why multi-parameter type classes?

The most visible extension to Haskell type classes that we discuss is support for multi-parameter type classes. The possibility of multi-parameter type classes has been recognized since the original papers on the subject (Kaes [1988], Wadler & Blot [1989]), and Gofer has always supported them. This section collects together examples of multi-parameter type classes that we have encountered. None of them are new, none will be surprising to the cognoscenti, and many have appeared *inter alia* in other papers. Our purpose in collecting them is to provide a shared database of motivating examples. We would welcome new contributions.

2.1 Overloading with coupled parameters

Concurrent Haskell (Peyton Jones, Gordon & Fine [1996]) introduces a number of types such as mutable variables `MutVar`, "synchronised" mutable variables `MVar`, channel variables `Chan`, communication channels `Channel`, and skip channels `SkipChan`, all of which come with similar operations that take the form:

```
newX :: a -> IO (X a)
getX :: X a -> IO a
putX :: X a -> IO ()
```

where `X` ranges over `MVar` etc. Here are similar operations in the standard state monad:

```
newST :: a -> ST s (MutableVar s a)
getST :: MutableVar s a -> ST s a
putST :: MutableVar s a -> a -> ST s ()
```

These are manifestly candidates for overloading; yet a single parameter type class can't do the trick. The trouble is that in each case the monad type and the reference type come as a pair: `(IO, MutVar)` and `(ST s, MutableVar s)`. What we want is a multiple parameter class that abstracts over both:

```
class Monad m => VarMonad m v where
  new :: a -> m (v a)
  get :: v a -> m a
  put :: v a -> a -> m ()
```

instance `VarMonad IO MutVar` where ...
instance `VarMonad (ST s) (MutableVar s)` where ...

This is quite a common pattern, in which a two-parameter type class is needed because the class signature is really over a tuple of types and where instance declarations capture direct relationships between specific tuples of type constructors. We call this *overloading with coupled parameters*.

Here are a number of other examples we have collected:

```
class Monad m => StateMonad m s where
  gets :: m s
  puts :: s -> m ()
  VarMonad example:
  around naked, instead of inside a container as in the
  class StateMonad (Jones [1995]) carries the state
```

Here the monad `m` carries along a state of type `s`; `gets` extracts the state from the monad, and `puts` overwrites the state with a new value. One can then define instances of `StateMonad`.

```
newType State s a = State (s -> (a,s))
instance StateMonad (State s) s where ...
```

Notice the coupling between the parameters arising from the repeated type variable `s`. Jones [1995] also defines a related class, `ReaderMonad`, that describes computations that read some fixed environment

```
class Monad m => ReaderMonad m e where
  env :: e -> m a
  getEnv :: m e
```

`newType Env e a = Env (e -> a)`
instance `ReaderMonad (Env e) e` where ...

• Work in Glasgow and the Oregon Graduate Institute on hardware description languages has led to class decorations similar to this:

```
class Monad ct => Hard ct sg where
  const :: a -> ct (sg a)
  opl :: (a -> b) -> sg a -> ct (sg b)
  op2 :: (a -> b -> c) -> sg a -> sg b -> ct (sg c)
```

instance `Hard NetCircuit NetSignal` where ...
instance `Hard SimCircuit SimSignal` where ...

Here, the circuit constructor, `ct` is a monad, while the signal constructor, `sg`, serves to distinguish values available at circuit-construction time (of type `Int`, say) from those flowing along the wires at circuit-execution time (of type `SimSignal Int`, say). Each instance of `Hard` gives a different interpretation of the circuit; for example, one might produce a net list, while another might simulate the circuit.

Like the `VarMonad` example, the instance type come as a pair: it would make no sense to give an instance for `Hard NetCircuit SimSignal`.

• The Haskell prelude defines the following two functions for reading and writing files

```
readFile :: FilePath -> IO String
writeFile :: FilePath -> String -> IO ()
```

Similar functions can be defined for many more pairs of device handles and communicable types, such as mice, buttons, timers, windows, robots, etc.

```
readMouse :: Mouse -> IO MouseEvent
readButton :: Button -> IO ()
readTimer :: Timer -> IO Float
sendWindow :: Window -> Picture -> IO ()
sendRobot :: Robot -> Command -> IO ()
sendTimer :: Timer -> Float -> IO ()
```

These functions are quite similar to the methods `get :: VarMonad r m => r a -> m a` and `put :: VarMonad r m => r a -> m ()` of the `VarMonad` family, except that here the monad `m` is fixed to `IO` and the choice of the value type `a` is coupled with the box type `v a`. So what we need here is a multi-parameter class that overloads on `v a` and `a` instead:

```
class IODevice handle a where
  receive :: handle -> IO a
  send :: handle -> a -> IO a
```

(Perhaps one could go one step further and unify class `IODevice r a` and class `Monad m => StateMonad m r` into a three parameter class `Monad m => Device m r a`.)

²This example was suggested by Enno Scholz.

• An appealing application of type classes is to describe mathematical structures, such as groups, fields, monoids, and so on. But it is not long before the need for coupled overloading arises. For example:

```
class (Field k, AdditiveGroup a)
  => VectorSpace k a where
  @* :: k -> a -> a
```

Here the operator @* multiplies a vector by a scalar.

2.2 Overloading with constrained parameters

Libraries that implement sets, bags, lists, finite maps, and so on, all use similar functions (empty, insert, union, lookup, etc). There is no commonly-agreed signature for such libraries that usefully exploits the class system. One reason for this is that multi-parameter type classes are absolutely required to do a good job. Why? Consider this first attempt:

```
class Collection c where
  empty :: c
  insert :: a -> c a
  union :: c a -> c a -> c a
  ...etc...
```

The trouble is that *the type variable a is universally quantified* in the signature for insert, union, and so on. This means we cannot use equality or greater-than on the elements, so we cannot make sets an instance of Collection, which rather defeats the object of the exercise. By far the best solution is to use a two-parameter type class, thus:

```
class Collection c a where
  empty :: c a
  insert :: a -> c a -> c a
  union :: c a -> c a -> c a
  ...etc...
```

The use of a multi-parameter class allows us to make instance declarations that constrain the element type on a per-instance basis:

```
instance Eq a => Collection ListSet a where
  empty = ...
  insert a xs = ...
  ...etc...
instance Ord a => Collection TreeSet a where
  empty = ...
  insert x t = ...
  ...etc...
```

The point is that different instance declarations can constrain the element type, a, in different ways. One can look at this as a variant of coupled-parameter overloading (discussed in the preceding section). Here, the second type in the pair is *constrained* by the instance declaration (e.g. "Ord a => ..."), rather than *completely specified* as in the previous section. In general, in this form of overloading, one or more of the parameters in any instance is a variable that

³This example was suggested by Sergey Mechveliani.

One can also construct applications for multi-parameter classes where the relationships between different parameters are much looser than in the examples that we have seen above. After all, in the most general setting, a multi-parameter type class C could be used to represent an arbitrary relation between types where, for example, (a, b) is in the relation if, and only if, there is an instance for (C a b).

- One can imagine defining an isomorphism relationship between types (Liang, Hudak & Jones [1995]):

```
class Iso a b where
  iso :: a -> b
  osi :: b -> a
instance Iso a a where iso = id
```

- One could imagine overloading Haskell's field selectors by declaring a class

```
class Hasf a b where
  f :: a -> b
```

for any field label f. So if we have the data type Foo = Foo{foo :: Int}, we would get a class declaration class Hasfoo a b where foo :: a -> b and an instance declaration

```
instance Hasfoo Foo Int where
  foo (Foo foo) = foo
```

This is just a cut-down version of the kind of extensible records that were proposed by Jones [1994]).

These examples are "looser" than the earlier ones, because the result types of the class operations do not mention all the class type variables. In practice, we typically find that such relations are too general for the type class mechanisms, and that it becomes remarkably easy to write programs whose overloading is ambiguous.

For example, what is the type of iso 'a' == iso 'b'? The iso function is used at type Char -> b, and the resulting values of iso 'a' and iso 'b' are compared with (==) used at type b -> b -> Bool. However this intermediate type is completely unconstrained and hence the resulting type, (Eq b, Iso Char b) => Bool, is ambiguous. One runs into similar problems quickly when trying to use overloading of field selectors. We discuss ambiguity further in Section 3.7.

2.4 Summary

In our view, the examples of this section make a very persuasive case for multi-parameter type classes, just as `Monad` and `Functor` did for constructor classes. These examples cry out for Haskell-style overloading, but it simply cannot be done without multi-parameter classes.

3 Background

In order to describe the design choices related to type classes we must briefly review some of the concepts involved.

3.1 Inferred contexts

When performing type inference on an expression, the type checker will infer (a) a monotype, and (b) a *context*, or set of *constraints*, that must be satisfied. For example, consider the expression:

```

\xs -> case xs of
  [] -> False
  (y:ys) -> y < z || (y==z && ys==[z])

```

Here, the type checker will infer that the expression has the

```

Context: {Ord a, Eq a, Eq [a]}
Type: [a] -> Bool

```

The constraint `Ord a` arises from the use of `>` on an element of the list, `y`; the constraint says that the elements of the list must lie in class `Ord`. Similarly, `Eq a` arises from the use of `==` on a list element. The constraint `Eq [a]` arises from the use of `==` on the tail of the list; it says that lists of elements of type `a` must also lie in `Eq`.

These typing constraints have an operational interpretation that is often helpful, though it is not required that a Haskell implementation use this particular operational model. For each constraint there is a corresponding *dictionary*—a collection of functions that will be passed to the overloaded operator involved. In our example, the dictionary for `Eq [a]` will be a tuple of methods corresponding to the class `Eq`. It will be passed to the second overloaded `==` operator, which will simply select the `==` method from the dictionary and apply it to `ys` and `[z]`. You can think of a dictionary as concrete, run-time “evidence” that the constraint is satisfied.

3.2 Context reduction

Contexts can be simplified, or *reduced*, in three main ways:

1. *Eliminating duplicate constraints.* For example, we can reduce the context `{Eq τ, Eq τ}` to just `{Eq τ}`.
2. *Using an instance declaration.* For example, the Haskell Prelude contains the standard instance declaration:

```

instance Eq a => Eq [a] where ...

```

[†]Notice that in `(inst)`, `C` and `P` appear in the same order on the top and bottom lines of the rules, whereas they are reversed in `(super)`. This suggests an infelicity in Haskell's syntax, but one that it is perhaps too late to correct!

```

{Ord a, Eq a} -> {Ord a}

```

More precisely, we say that `Q entails P`, written `Q ⊨ P`, if the constraints in `P` are implied by those in `Q`. We define the meaning of class constraints more formally using the definition of the entailment relation defined in Figure 1. The first two rules correspond to (2) and (3) above. The substitution `θ` maps type variables to types; it allows class and instance declarations to be used at substitution-instances of their types. For example, from the declaration

```

instance Eq a => Eq [a] where ...

```

we can perform the following context reduction: we can read this as saying that each `Ord` dictionary contains an `Eq` dictionary as a sub-component. So the constraint `Eq a` is implied by `Ord a`, and it follows that we can perform the following context reduction:

```

class Eq a => Ord a where ...

```

3. *Using a class declaration.* For example, the class declaration for `Ord` in the Haskell Prelude specifies that `Eq` is a superclass of `Ord`:
- We say that a constraint *matches* an instance declaration if there is a substitution of the type variables in the instance declaration head that makes it equal to the constraint.

```

{Ord a, Eq a, Eq [a]} -> {Ord a, Eq a}

```

This instance declaration specifies how we can use an equality on values of type `a` to define an equality on lists of type `[a]`. In terms of the dictionary model, the instance declaration specifies how to construct a dictionary for `Eq [a]` from a dictionary for `Eq a`. Hence we can perform the following context reduction:

Figure 1: Rules for entailment

(inst)	$\frac{TV(P) \subseteq dom(\theta) \quad \text{instance } C \Rightarrow P \text{ where } \dots}{\theta(C) \sqsupseteq P}$
(super)	$\frac{TV(P) \subseteq dom(\theta) \quad \text{class } C \Rightarrow P \text{ where } \dots \quad \theta(P) \sqsupseteq \theta(C)}{\theta(P) \sqsupseteq P}$
(mono)	$\frac{\theta \subseteq P}{\theta \subseteq P}$
(trans)	$\frac{P \sqsupseteq Q \quad Q \sqsupseteq R}{P \sqsupseteq R}$

3.6 Overlapping instance declarations

Consider these declarations:

```
class MyShow a where
  myShow :: a -> String
```

What we mean by (b) is that it makes no difference whether context reduction is done just before generalising f , or just after inferring the type of the sub-expression $(ys==[z])$, or anywhere in between; all that matters is how much is done before generalisation.

Which of these types is inferred depends on how much context reduction is done before generalisation, a topic we discuss later (Section 4.3). For the present, we only need note (a) that there is a choice to be made here, and (b) that the time that choice is crystallised is at the moment of generalisation.

```
f :: (Ord a) => [a] -> Bool
f :: (Ord a, Eq a) => [a] -> Bool
f :: (Ord a, Eq a, Eq [a]) => [a] -> Bool
```

Having inferred a type for the right-hand side of f , the type checker must generalise this type to obtain the polymorphic type for f . Here are several possible types for f :

```
Let
  f = \xs -> case xs of
    [] -> False
    (y:ys) -> y > z ||
      (y==z && ys==[z])
  in
  ...
```

Suppose that the example in Section 3.1 is embedded in a larger expression:

3.5 Generalisation

If, on the other hand, overlapping instance declarations are permitted, then reducing a tautological constraint in this way is not legitimate, as we discuss in Section 4.4.

This declares the state transformer type, $ST\ s$, to be a monad, regardless of the type s .

```
instance Monad (ST s) where ...
```

Another example of one of these tautological constraints that contain type variables is given by this instance declaration:

and let us assume for the moment that overlapping instance declarations are prohibited (Section 4.4). Now suppose that the context $\{foo\ Int, t\}$ is subject to context reduction. Regardless of the type t , it can be simplified to $\{Eq\ Int\}$ (using the instance declaration above), and hence to $\{Int\}$ (using the Int instance for Eq). Even if t contains type variables, the constraint $foo\ (Int, t)$ can still be reduced to $\{Int\}$, so it is a tautological constraint.

```
instance Eq a => Foo (a, b) where ...
```

³In Gofor, an instance declaration $P \Rightarrow C$ where ... brings about the axiom $C \vdash P$, because the representation in Gofor of a dictionary for C contains sub-dictionaries for P . In retrospect, this was probably a poor design decision because it is not always very intuitive. Moreover, it was later discovered that this is incompatible with overlapping instances: while either one is acceptable on its own, the combination results in an unsound type system. The Gofor type system still suffers from this problem today because of concerns that removing support for either feature would break a lot of existing code.

It is less obvious that a tautological constraint does not have to be ground. Consider

3.4 Tautological constraints

A *tautological* constraint is one that is entailed by the empty context. For example, given the standard instance declarations, $Ord\ [Int]$ is a tautological constraint, because $Ord\ Int$ allow us to conclude that $\{\} \vdash \{Ord\ [Int]\}$.

Arguably, therefore, rather than reporting an error message, context reduction should be deferred (see Section 4.3), in the hope that an importing module will have the necessary information of even legitimate missing-instance error messages until the "main" module is compiled (when no further instance declarations can occur), which is quite a serious disadvantage. Furthermore, it is usually easy to arrange that "see" it. If this is so, then failure can be reported immediately, regardless of the context reduction strategy.

instance ... => Eq (Tree ...) where ...

Context reduction *fails*, and a type error is reported, if there is no instance declaration that can match the given constraint. For example, suppose that we are trying to reduce the constraint $Eq\ (Tree\ \tau)$, and there is no instance declaration of the form

3.3 Failure

The connection between entailment and context reduction is this: to reduce the context P to P' it is necessary (but perhaps not sufficient) that $P' \vdash P$. The reason that entailment is not sufficient for reduction concerns overlapping instances: there might be more than one P' with the property that $P' \vdash P$, so which should be chosen? Overlapping instance declarations are discussed in Section 3.6 and 4.4.

We can deduce that $\{Eq\ \tau\} \vdash \{Eq\ [\tau]\}$, for an arbitrary type τ . The remaining rules explain that entailment is monotonic and transitive as one would expect.

As we observed earlier, some programs have *ambiguous typings* where the result of the read might lead to different results. Programs with ambiguous typings are therefore rejected by Haskell.

3.7 The ambiguity problem

Notice that the argument of the `StateT` monad transformer is not `State Char` but rather the enriched monad `(ErrorT (State Char))`, assuming that `ErrorT` is another monad transformer. Now, the overloading mechanisms will automatically make sure that the first call to `update` in `f` takes place in the outermost `Int` state monad, while the second call will be lifted up from the depths of the innermost `Char` state monad.

```
type M = StateT Int (ErrorT (State Char))
```

Following: Later, we might call this function with an integer and a character argument on a monad that we've constructed using the

```
f :: (StateMonad m Int, StateMonad m Char) => Int -> Char -> m (Int,Char)
f x y = do x' <- update (const x)
         y' <- update (const y)
         return (x', y')
```

For example: Note the overlap with the previous instance declaration, which plays an essential role. Defining monad transformers in this way allows us to build up composite monads, with automatically generated liftings of the important operators.

```
instance (MonadT t, StateMonad m s) => StateMonad (t m) s where
  update f = lift (update f)
```

Critically, we also need to know that any properties enjoyed by the original monad, are also supported by the transformed monad. We can capture this formally using:

```
instance MonadT (StateT s) where ...
instance MonadT (StateT s) where ...
newtype StateT s m a = StateT (s -> m (a,s))
```

For example, the state monad transformer that can add state to any monad:

```
lift :: Monad m => m a -> t m a
class MonadT t where
```

To combine the features of monads we introduced a notion of a monad transformer; the idea is that a monad transformer `t` takes a monad `m` as an argument and produces a new monad `(t m)` as a result that provides all of the computational features of `m`, plus some new ones added in by the transformer `t`.

hence support a combination of different primitive features. This same approach has proved to be very flexible in other recent work (Jones [1995a]; Liang, Hudak & Jones [1995])."

"In fact, we will take a more forward-thinking approach and use the constructor class mechanisms to define different families of monads, each of which supports a particular collection of simple primitives. The benefit of this is that, later, we will want to consider monads that are simultaneously instances of several different classes, and

A second application of overlapping instance declarations arises when we try to define *monad transformers*. The idea is given by Jones [1995]:

3.6.2 Monad transformers

These instance declarations overlap with all other instances of `Functor`. (Whether this is the best way to explain that an instance of `Monad` has a natural definition of `map` is debatable.)

```
instance Monad m => Functor m where
  map f m = [f x | x <- m]
```

Now, in any instance of `Monad`, there is a sensible definition of `map`, an idea we could express like this:

```
class Functor f where
  map :: (a -> b) -> f a -> f b
```

```
class Monad m where
  (>>=) :: m a -> (a -> m b) -> m b
  return :: a -> m a
```

One application of overlapping instance declarations is to define "default methods". Haskell has the following standard classes:

3.6.1 "Default methods"

When, during context reduction, a constraint matches two overlapping instance declarations, which should be chosen? We will discuss this question in Section 4.1, but for now we address the question of whether or not overlapping instance declarations are useful. We give two further examples.

are illegal in Haskell, but permitted in Gofor. matches both `q1` and `q2`. Overlapping instance declarations are said to *overlap* if `q1` and `q2` are unifiable. This definition is equivalent to saying that there is a constraint `q` that

```
instance P1 => Q1 where ...
instance P2 => Q2 where ...
```

Here, the programmer wants to use a different method for `MyShow` when used at `[Char]` than when used at other types. We say that the two instance declarations *overlap*, because there exists a constraint that matches both. For example, the constraint `MyShow [Char]` matches both declarations. In general, two instance declarations

```
instance MyShow a => MyShow [a] where
  myShow = myShow1
instance MyShow [Char] where
  myShow = myShow2
```

f :: Num Char => Char -> Char

Type inference on f gives rise to the constraint (Num Char). If instance declarations are not globally visible, then we would be forced to defer context reduction. In case f is called in another module that has an instance declaration for (Num Char). Thus we would have to infer the following type for f:

f x = 'c' + x

For example, consider a constraint that cannot match any instance declaration. Fourthly, we will assume that, despite separate compilation, instance declarations are globally visible. The reason for this is that we want to be able to report an error if we encounter a constraint that cannot match any instance declaration.

- If $P \Rightarrow \tau$ is a type, then $TV(P) \subseteq TV(\tau)$. If the context P mentions any type variables not used in τ then any use of a value with this type is certain to be ambiguous.

Thirdly, we require the following rule for types:

We discuss the design choices related to instance declarations in Sections 4.3 and 4.7.

- $TV(P) \subseteq \bigcup TV(\tau_i)$: that is, the instance context must not mention any type variables that are not mentioned in the instance types.

We call P the instance context, τ_1, \dots, τ_n the instance types, and $C \tau_1 \dots \tau_n$ the head of the instance declaration. Like Haskell, we insist that:

instance $P \Rightarrow C \tau_1 \dots \tau_n$ where ...

Next, we give rules governing instance declarations, which have the form:

- There can be at most one class declaration for each class C .
- Throughout the program, all uses of C are applied to n arguments.
- $\alpha_1 \dots \alpha_n$ must be distinct type variables.
- $TV(P) \subseteq \{\alpha_1, \dots, \alpha_n\}$. That is, P must not mention any type variables other than the α_i .
- The superclass hierarchy defined by the set of class declarations must be acyclic. This restriction is not absolutely necessary, but the applications for cyclic class structures are limited, and it helps to keep things simple.

(If multi-parameter type classes are prohibited, then $n = 1$). If $S \beta_1 \dots \beta_m$ is one of the constraints appearing in the context P , we say that S is a superclass of C . We insist on the following:

class $P \Rightarrow C \alpha_1 \dots \alpha_n$ where { op :: $\alpha_i \Rightarrow \tau_i$; ... }

Next, we give some ground rules about the form of class declarations. A class declaration takes the form:

The last point needs a little explanation. We have already seen that the way in which context reduction is performed affects the dynamic semantics of the program via the construction and use of dictionaries (other operational models will experience similar effects). It is essential that the way in which the typing derivation is constructed (there is usually more than one for a given program) should not affect the meaning of the program.

- We want to retain Haskell programs to remain legal, and to have the same meaning.
- We seek a coherent type system: that is, every different valid typing derivation for a program leads to a resulting program that has the same dynamic semantics.
- We want type inference to be decidable: that is, the compiler must not fail to terminate.
- We want to retain the possibility of separate compilation.
- We want all existing Haskell programs to remain legal, and to have the same meaning.
- We seek a coherent type system: that is, every different valid typing derivation for a program leads to a resulting program that has the same dynamic semantics.

Type systems are a huge design space, and we only have space to explore part of it in this paper. In this section we briefly record some design decisions currently embodied in Haskell that we do not propose to meddle with. Our first set of ground rules concern the larger setting:

4.1 The ground rules

We are now ready to discuss the design choices that must be embodied in a type-class system of the kind exemplified by Haskell. Our goal is to describe a design space that includes Haskell, Gofor, and a number of other options beside. While we express opinions about which design choices we prefer, our primary goal is to give a clear description of the design space, rather than to prescribe a particular solution.

4 Design choices

If no workable solution to the ambiguity problem has been found for single parameter classes, we are not optimistic that one will be found for multi-parameter classes.

Preliminary experience, however, is that multi-parameter type classes give new opportunities for ambiguity. Is there any way to have multi-parameter type classes without risking ambiguity? Our answer here is "no". One approach that has been suggested to the ambiguity problem in single-parameter type classes is to insist that all class operations take as their first argument a value of the class type (Ord-sky, Wadler & Wehr [1995]). Though it is theoretically attractive, there are too many useful classes that disobey this constraint (Num, for example, and overloaded constants in general), so it has not been adopted in practice. It is also not clear what the rule would be when we move to constructor classes, so that the class's "type" variable ranges over type constructors.

Instead, what we really want to report an immediate error when type-checking f.

So, if instance declarations are not globally visible, many missing-instance errors would only be reported when the main module is compiled, an unacceptable outcome. (Explicit type signatures might force earlier error reports, however.) Hence our ground rule. In practice, though, we can get away with something a little weaker than insisting that every instance declaration is visible in every module — for example, when compiling a standard library one does need instance declarations for unrelated user-defined types.

Lastly, we have found it useful to articulate the following principle:

- Adding an instance declaration to well-typed program should not alter either the static or dynamic semantics of the program, except that it may give rise to an overlapping-instance-declaration error (in systems that prohibit overlap).

4.2 Decision 1: the form of types

Decision 1: what limitations, if any, are there on the form of the context of a type? In Haskell 1.4, types (whether inferred, or specified in a type signature) must be of the form $P \Rightarrow \tau$, where P is a simple context. We say that a context is simple if all its constraints are of the form $C \alpha$, where C is a class and α is a type variable.

This design decision was defensible for Haskell 1.2 (which lacked constructor classes) but seems demonstrably wrong for Haskell 1.4. For example, consider the definition:

```
g = \xs -> (map not xs) == xs
```

The right hand side of the definition has the type $f \text{ Bool} \rightarrow \text{Bool}$, and context $\{ \text{Functor } f, \text{Eq } (f \text{ Bool}) \}$. Because of the second constraint here, this cannot be reduced to a simple context by the rules in Figure 1, and Haskell 1.4 rejects this definition as ill-typed. In fact, if we insist that the context in a type must be simple, the function g has many legal types (such as $[\text{Bool}] \rightarrow \text{Bool}$), but no *principal*, or most general, type. If, instead, we allow non-simple contexts in types, then it has the perfectly sensible principal type:

```
g :: (Functor f, Eq (f Bool)) => f Bool -> Bool
```

In short, Haskell 1.4 lacks the principal type property, namely that any typable expression has a principal type; but it can be regained by allowing richer contexts in types. This is not just a theoretical nicety — it directly affects the expressiveness of the language.

⁶The definition of the class Functor was given in Section 3.6.1.

Similar problems occur with multi-parameter classes if we insist that the arguments of each constraint in a context must be variables — a natural generalization of the single-parameter notion of a simple context. For example, one can imagine inferring a context such as $\{ \text{StateMonad IO } \alpha \}$, where α is a type variable. If we then want to generalise over α , we would obtain a function whose type was of the form $\text{StateMonad IO } \alpha \Rightarrow \tau$. If such a type was illegal then, as with the previous example, we would be forced to reject the program even though it has a sensible principal type in a slightly richer system.

The choices for the allowable contexts in types seem to be:

- Choice 1a (Haskell): the context of a type must be simple (with some extended definition of "simple").
- Choice 1b (Göfer): there are no restrictions on the context of a type.
- Choice 1c: something in between these two. For example, we might insist that the context in a type is reduced "as much as possible". But then a legal type signature might become illegal if we introduced a new instance declaration (because then the type signature might no longer be reduced as much as possible).

4.3 Decision 2: How much context reduction?

Decision 2: how much context reduction should be done before generalisation? Haskell and Göfer make very different choices here. Haskell takes an eager approach to context reduction, doing as much as possible before generalisation, while Göfer takes a lazy approach, only using context reduction to eliminate tautological constraints.

It turns out that this choice has a whole raft of consequences, as Jones [1994, Chapter 7] discusses in detail. These consequences mainly concern pragmatic matters, such as the complexity of types, or the efficiency of the resulting program. It is highly desirable that the choice of how much context reduction is done when should not affect the meaning of the program. It is bad enough that the meaning of the program inevitably depends on the resolution of overload-ing (Odersky, Wadler & Wehr [1995]). It would be much worse if the program's meaning depended on the exact way in which the overloading was resolved — that is, if the type system were incoherent (Section 4.1).

Here, then, are the issues affecting context reduction.

1. Context reduction usually leads to "simpler" contexts, which are perhaps more readily understood (and written) by the programmer. In our earlier example, $\text{Ord } a$ is simpler than $\{ \text{Ord } a, \text{Eq } a, \text{Eq } [a] \}$.

Occasionally, however, a "simpler" context might be less "natural". Suppose we have a data type Set with an operation union, and an Ord instance (Jones [1994, Section 7.1]):

⁶The definition of the class Functor was given in Section 3.6.1.

```
f :: Ord a => [a] -> a -> Bool
```

A dictionary for Ord a will be passed to f, which will construct a dictionary for Ord [a]. In this example, though, f is called twice, at the same type, and the two calls will independently construct the same Ord [a] dictionary. We could obtain more sharing (i.e. efficiency) by postponing the context reduction, inferring instead the following type for f:

```
f :: Ord [a] => [a] -> a -> Bool
```

Now f is passed a dictionary for Ord [a], and this dictionary can be shared between the two calls of f.

Because context reduction is postponed until the top level in Gofor, this sharing can encompass the whole program, and only one dictionary for each class/type combination is ever constructed.

5. *Type signatures interact with context reduction.*

Haskell allows us to specify a type signature for a function. Depending on how context reduction is done, and what contexts are allowed in type signatures, this type might be more or less reduced than the inferred type. For example, if full context reduction is normally done before generalisation, then is this a valid type signature?

```
f :: Eq [a] => ...
```

That is, can a type signature decrease the amount of context reduction that is performed? In the other direction, if context reduction is not usually done at generalisation, then is this a valid type signature?

```
f :: Eq a => ...
```

where f's right-hand side generates a constraint Eq [a]? That is, can a type signature increase the amount of context reduction that is performed?

6. *Context reduction is necessary for polymorphic recursion.*

One of the new features in Haskell 1.4 is the ability to define a recursive function in which the recursive call is at a different type than the original call. A feature that has proved itself useful in the efficient encoding of functional data structures (Okasaki [1996]). For example, consider the following non-uniformly recursive function:

```
f :: Eq a => a -> a -> Bool
  f x y = if x == y then True
        else f [x] [y]
```

It is not possible to avoid all runtime dictionary construction in this example, because each call to recursive f must use a dictionary of higher type, and there is no static bound to the depth of recursion. It follows that the strategy of deferring all context reduction to the top level, thereby ensuring a finite number of dictionaries, cannot work. The type signature is necessary for the type checker to permit polymorphic recursion, and it in turn forces reduction of the constraint Eq [a] that arises from the recursive call to f.

```
data Set a = ...
```

```
union :: Eq a => Set a -> Set a -> Set a
```

```
instance Eq a => Ord (Set a) where ...
```

Now, consider the following function definition:

```
f x y = if (x<y) then y else x 'union' y
```

With context reduction, f's type is inferred to be

```
f :: Eq a => Set a -> Set a -> Set a
```

whereas without context reduction we would infer

```
f :: Ord (Set a) => Set a -> Set a -> Set a
```

One can argue that the latter is more "natural" since it is clear where the Ord constraint comes from, while the former contains a slightly surprising Eq constraint that results from the unrelated instance declaration.

7. *Context reduction often, but not always, reduces the number of dictionaries passed to functions.*

In the running example of Section 3, doing context reduction before generalisation allowed us to pass one dictionary to f instead of three.

Sometimes, though, a "simpler" context might have more constraints (i.e. more dictionaries to pass in a dictionary-passing implementation). For example, given the instance declaration:

```
instance (Eq a, Eq b) => Eq (a,b) where ...
```

the constraint Eq (a,b) would reduce to {Eq a, Eq b}, which may be "simpler", but certainly is not shorter.

3. *Context reduction eliminates tautological constraints.*

For example, without context reduction the function

```
double = \x -> x + (x::Int)
```

would get the type

```
double :: Num Int => Int -> Int
```

This type means that a dictionary for Num Int will be passed to double, which is quite redundant. It is invariably better to reduce {Num Int} to {}, using the Int instance of Num. The "evidence" that Int is an instance of Num takes the form of a global constant dictionary for Num Int. (This example uses a ground constraint, but the same reasoning applies to any tautological constraint.)

4. *Delaying context reduction increases sharing of dictionaries.*

Consider this example:

```
let
  f xs y = xs > [y]
in
  f xs y && f xs z
```

Haskell will infer the type of f to be:

We should note that 2b-rule out Choice 1a for type signatures. Furthermore (as we shall see in Section 4.4), Choices 2a and 2e rule out overlapping instance declarations. The intent in Choice 2e is to leave as much flexibility as possible to the compiler (so that it can make the most efficient choice) while still giving a well-defined static and dynamic semantics for the language:

- So far as the static semantics is concerned, when context reduction is performed does not change the set of typable programs.
- Concerning the dynamic semantics, in the absence of overlapping instance declarations, a given constraint can only match a unique instance declaration.

4.4 Decision 3: overlapping instance declarations

Decision 3: are instance declarations with overlapping (but not identical) instance types permitted? (See Section 3.6.)

If overlapping instances are permitted, we need a rule that specifies which instance declaration to choose if more than one matches a particular constraint. Gofers' rule is that the declaration that matches most closely is chosen. In general, further rules are required to disambiguate the choice — for example, Gofers requires that instance declarations may only overlap if one is a substitution instance of the other. Unfortunately, this is not enough. As we mentioned above, there is a fundamental conflict between eager (or unspecified) context reduction and the use of overlapping instances. To see this, consider the definition:

```
let
  f x = myShow (x+++x)
  in
  (f "c", f [True,False])
```

where myShow was defined in Section 3.6. If we do (full) context reduction before generalising f, we will be faced with a constraint myShow [a], arising from the use of myShow. Unfortunately the eager context reduction we must simplify it, presumably using the instance declaration for myShow [a], to obtain the type

```
f :: MyShow a => a -> String
```

If we do so, then every call to f will be committed to the myShow1 method. However, suppose that we first perform a simple program transformation, inlining f at both its call sites, to obtain the expression:

```
(myShow "c", myShow [True,False] [True,False])
```

Now the two calls distinct calls to myShow will lead to the constraints myShow [Char] and myShow [Bool] respectively; the first will lead to a call of myShow2 while second will lead to a call of myShow1. A simple program transformation has changed the behaviour of the program!

7. Context reduction affects typability. Consider the following (continued) program:

```
data Tree a = Nil | Fork (Tree a) (Tree a)
  let silly y = (y==Nil)
      in x + 1
```

If there is no Eq instance of Tree, then the program is arguably erroneous, since silly performs equality at type Tree. But if context reduction is deferred, silly will, without complaint, be assigned the type

```
silly :: Eq (Tree a) => a -> Bool
```

Then, since silly is never called, no other type error will result. In short, the definition of which programs are typable and which are not depends on the rules for context reduction.

8. Context reduction conflicts with the use of overlapping instances. This is a bigger topic, and we defer it until Section 4.4.

Bearing in mind this (amazingly large) set of issues, there seem to be the following possible choices:

Choice 2a (Haskell, eager): reduce every context to a simple context before generalisation. However, as we have seen, this may mean that some perfectly reasonable programs are rejected as being ill-typed.

Choice 2b (lazy): do no context reduction at all until the constraints for the whole program are gathered together; then reduce them. This is satisfyingly decisive, but it gives rise to pretty stupid types, such as:

```
(Eq a, Eq a) => a -> Bool
(Mum Int, Show Int) => Int -> String
```

Choice 2c (Gofers, fairly lazy): do context reduction before generalisation, but refrain from using rule (inst) except for tautological constraints. If overlapping instances are permitted, then change "tautological" to "ground". A variant would be to refrain from using (super) as well.

Choice 2d (Gofers + polymorphic recursion): like 2c, but with the added rule that if there is a type signature, the inferred context must be entailed by the content in the type signature, and the variable being defined is assigned the type in the signature throughout its scope. This is enough to make the choice compatible with polymorphic recursion, which 2c is not.

Choice 2e (relaxed): leave it unspecified how much context reduction is done before generalisation! That is, if the actual context of the term to be generalised is P, then the inferred context for the generalised term P' reduces to. The same rule for type signatures must apply as in 2d, for the same reason. To avoid the problem of item 7 we can require that an error is reported as soon as a generalisation step encounters a constraint that cannot possibly be satisfied (even if that constraint is not reduced).

Now consider the original program again. If instead we deferred context reduction we would infer the type:

```
f :: MyShow [a] => a -> String
```

Now the two calls to `f` will lead to the constraints `MyShow [Char]` and `MyShow [Bool]` as in the inlined case, leading to calls to `myShow2` and `myShow1` respectively. In short, eager context reduction in the presence of overlapping instance declarations can lead to premature commitment to a particular instance declaration, and consequential loss of simple source-language program transformations.

Overlapping instances are also incompatible with the reduction of non-ground tautological constraints. For example, suppose we have the declaration

```
Instance Monad (ST s) where ...
```

and we are trying to simplify the context `{Monad (ST τ)}`. It would be wrong to reduce it to `{}` because there might be an overlapping instance declaration

```
Instance Monad (ST Int) where ...
```

This inability to simplify non-ground tautological constraints has, in practice, caused Gofor some difficulties when implementing lazy state threads (Launuchbury & Peyton Jones [1995]). Briefly, `runST` insists that its argument has type `$\forall \alpha. ST \alpha \tau$` , while the argument type would be inferred to be `Monad (ST α) => ST \alpha \tau`.

To summarise, if overlapping instances are permitted, then the meaning of the program depends in detail on when context reduction takes place. To avoid loss of coherence, we must specify when context reduction takes place as part of the type system itself.

One possibility is to defer reduction of any constraint that can possibly match more than one instance declaration. That restores the ability to perform program transformations, but it interacts poorly with separate compilation. A separately-compiled library might not "see" all the instances of a given class that a client module uses, and so must conservatively assume that no context reduction can be done at all on any constraint involving a type variable.

So the only reasonable choices are these:

Choice 3a: prohibit overlapping instance declarations.

Choice 3b: permit instance declarations with overlapping, but not identical, instance types, provided one is a substitution instance of the other; but restrict all uses of the `(inst)` rule (Figure 1) to ground contexts `C, P`.

This condition identifies constraints that can match at most one instance declaration, regardless of what further instance declarations are added.

4.5 Decision 4: instance types

Decision 4: in the instance declaration

```
Instance P => C  $\tau_1 \dots \tau_n$  where ...
```

what limitations, if any, are there on the form of the instance types, $\tau_1 \dots \tau_n$?

⁷Suggested by John Matthews.

Another reason for wanting non-simple instance types is Instance Num a => Num (Ratio a) where ... Instance (Liftable f, Num a) => Num (f a) where ...

The instance declaration is entirely reasonable: it says that any "liftable" type constructor `f` can be used to construct a new numeric type `(f a)` from an existing numeric type `a`. Indeed, these declarations precisely generalises the Behaviour class of Elliott & Hudak [1997], and we have encountered other examples of the same pattern. (You will probably have noticed that `Lift1` is just the map from the `Liftable` class; perhaps `Functor` should be a superclass of `Liftable`.) A disadvantage of `Liftable` is that now the Haskell types for `Complex` and `Ratio` must be made instances of `Num` indirectly, by making them instances of `Liftable`. This seems to work fine for `Complex`, but not for `Ratio`. Incidentally, we could overcome this problem if we had overlapping instances, thus:

```
class Liftable f where
  lift0 :: a -> f a
  lift1 :: (a->b) -> f a -> f b
  lift2 :: (a->b->c) -> f a -> f b -> f c
instance (Liftable f, Num a) => Num (f a) where
  fromInteger = lift0 . fromInteger
  negate = lift1 negate
  (+) = lift2 (+)
```

We have come across examples where it makes sense for the instance types not to be simple types. Section 3.6.1 gave examples in which the instance type was just a type variable, although this was in the context of overlapping instance declarations. Here is another example⁷:

```
Foo (Tree  $\alpha$ ) => \tau
```

(Note that these two do not overlap.) Given the constraint `(Foo (Tree α))`, for some type variable `α` , we cannot decide which instance declaration to use until we know more about `α` . If we are generalising over `α` , we will therefore end up with a function whose type is of the form

```
Instance Foo (Tree Int) where ...
Instance Foo (Tree Bool) where ...
```

For example, suppose we had:
declaration might be a potential match for the constraint.
be other than a type variable then more than one instance
which case an error can be signalled). If τ were allowed to
restriction to simple contexts in types (Section 4.2). Why?
variables. This decision is closely bound up with Haskell's
where T is a type constructor and $\alpha_1 \dots \alpha_n$ are distinct type
 τ is a simple type; that is, a type of the form $T \alpha_1 \dots \alpha_n$,
 $n = 1$. Furthermore, Haskell insists that the single type
Haskell 1.4 has only single-parameter type classes, hence

when using old types for new purposes. For example⁸, suppose we want to define the class of moveable things:

```
class Moveable t where
  move :: Vector -> t -> t
```

Now let us make points moveable. What is a point? Perhaps just a pair of Floats. So we might want to write

```
instance Moveable (Float, Float) where ...
```

or even

```
type Point = (Float, Float)
```

```
instance Moveable Point where ...
```

Unlike the Listable example, it is possible to manage with simple instance types, by making Point a new type:

```
newtype Point = MkPoint Float Float
```

```
instance Moveable Point where ...
```

but that might be tiresome (for example, unzip split a list of points into their x-coordinates and y-coordinates).

Choice 4a (Haskell): the instance type(s) τ_i must all be simple types.

Choice 4b: each of the instance types τ_i is a simple type or a type variable, and at least one is not a type variable. (The latter restriction is necessary to ensure that context reduction terminates.)

Choice 4c: at least one of the instance types τ_i must not be a type variable.

Choice 4c would permit the Listable example above. It would also permit the following instance declarations

```
instance D (T Int a) where ...
instance D (T Bool a) where ...
```

even if overlapping instances are prohibited (provided, of course, there was no instance for D (T a b)). It would also allow strange-looking instance declarations such as

```
instance C [[a -> Int]] where ...
```

which in turn make the matching of a candidate instance declaration against a constraint a little more complicated (although not much).

If overlapping instances are permitted, then it is not clear whether choices 4b and 4c lead to a decidable type system. If overlapping instances are not permitted then, seem to be no technical objections to them, and the examples given above suggest that the extra expressiveness is useful.

4.6 Decision 5: repeated type variables in instance heads

Decision 5: in the instance declaration

```
instance P => C  $\tau_1 \dots \tau_n$  where ...
```

⁸Suggested by Simon Thompson.

can the instance head τ_i contain repeated type variables? This decision is really part of Decision 4 but it deserves separate treatment.

Consider this instance declaration, which has a repeated type variable in the instance type:

```
instance ... => Foo (a, a) where ...
```

In Haskell this is illegal, but there seems no technical reason to exclude it. Furthermore, it is useful: the VarMonad instance for ST in Section 2.1 used repeated type variables, as did the Iso example in Section 2.3.

Permitting repeated type variables in the instance type of an instance declaration slightly complicates the process of matching a candidate instance declaration against a constraint, requiring full matching (i.e. one-way unification, a well-understood algorithm). For example, when matching the instance head $\text{Foo } (\alpha, \alpha)$ against a constraint $\text{Foo } (\tau_1, \tau_2)$ one must first bind α to τ_1 , and then check for equality between the now-bound α and τ_2 .

Choice 5a: permit repeated type variables in an instance head.

Choice 5b: prohibit repeated type variables in an instance head.

4.7 Decision 6: instance contexts

Decision 6: in the instance declaration

```
instance P => C  $\tau_1 \dots \tau_n$  where ...
```

what limitations, if any, are there on the form of the instance context, P ?

As mentioned in Section 4.1, we require that $\text{TV}(P) \subseteq \bigcup \text{TV}(\tau_i)$. However, Haskell has a more drastic restriction: it requires that each constraint in P be of the form $C \alpha$ where α is a type variable. An important motivation for a restriction of this sort is the need to ensure termination of context reduction. For example, suppose the following declaration was allowed:

```
instance C [[a]] => C [a] where ...
```

The trouble here is that for context reduction to terminate it must reduce a context to a simpler context. This instance declaration will "reduce" the constraint $(C [\tau])$ to $(C [[\tau]])$, which is more complicated, and context reduction will diverge. Although they do not seem to occur in practical applications, instance declarations like this are permitted in Gofer—with the consequence that its type system is in fact undecidable.

In short, it is essential to place enough constraints on the instance context to ensure that context reduction converges. To do this, we need to ensure that something "gets smaller" in the passage from $C \tau_1 \dots \tau_n$ to P . Haskell's restriction to simple contexts certainly ensures termination, because the argument types are guaranteed to get smaller. In principle, instance declarations with irreducible but non-simple contexts might make sense:

⁸Suggested by Simon Thompson.

Instance Monad (t m) => Foo t m where ...

We have yet to find any convincing examples of this. However, if context reduction is deferred (Choices 2b,c) then we must permit non-simple instance contexts. For example:

```
data Tree a = Node a [Tree a]
Instance (Eq a, Eq [Tree a]) => Eq (Tree a) where
  (==) (Node v1 ts1) (Node v2 ts2)
    = (v1 == v2) && (ts1 == ts2)
```

Here, if we are not permitted to reduce the constraint Eq [Tree a], it must appear in the instance context.

Lastly, if the constraints in P involve only type variables, when multi-parameter type classes are involved we must also ask whether a single constraint may contain a repeated type variable, thus:

```
Instance Foo a a => Baz a where ...
```

There seems to be no technical reason to prohibit this.

Choice 6a: constraints in the context of an instance declaration must be of the form $C \alpha_1 \dots \alpha_n$, with the α_i distinct.

Choice 6b: as for Choice 6a, except without the requirement for the α_i to be distinct.

Choice 6c: something less restrictive, but with some way of ensuring decidability of context reduction.

4.8 Decision 7: what superclasses are permitted

Decision 7: in a class declaration,

```
class P => C \alpha_1 \dots \alpha_n where { op :: Q => T ; ... }
```

what limitations, beyond those in Section 4.1, are there on the form of the superclass context, P ? Haskell restricts P to consist of constraints of the form $D \beta_1 \dots \beta_m$, where β_i must be a member of $\{\alpha_1, \dots, \alpha_n\}$, and all the β_i must be distinct. But what is wrong with this?

```
class Foo (t m) => Baz t m where ...
```

Also in this case, there seems to be no technical reason to prohibit this.

Choice 7a: constraints in the superclass context must be as in Haskell, i.e. the constraints are of the form $D \alpha_1 \dots \alpha_n$, with the α_i distinct, and a subset of the type variables that occur in the class head.

Choice 7b: no limitations on superclass contexts, except those postulated in Section 4.1.

4.9 Decision 8: improvement

Suppose that we have a constraint with the following properties:

- it contains free type variables;
- it does not match any instance declaration⁹
- it can be made to match an instance declaration by instantiating some of the constraint's free type variables;
- no matter what other (legal) instance declarations are added, there is only one instance declaration that the constraint can be made to match in this way.

If all these things are true, an attractive idea is to improve the constraint by instantiating the type variables in the constraint so that it does match the instance declaration. This makes some programs typable that would not otherwise be so. It does not compromise any of our principles, because the last condition ensures that even adding new instance declarations will not change the way in which improvement is carried out.

Choice 8a: no improvement.

Choice 8b: allow improvement in some form.

Choice 8b would obviously need further elaboration before this design decision is crisply formulated.

4.10 Decision 9: Class declarations

Decision 9: what limitations, if any, are there on the contexts in class-member type signatures? Presumably class-member type signatures should obey the same rules as any other type signature, but Haskell adds an additional restriction. Consider:

```
class C a where
  op1 :: a -> a
  op2 :: Eq a => a -> a
```

In Haskell, the type signature for `op2` would be illegal, because it further constrains the class type variable `a`. There seems to be no technical reason for this restriction. It is simply a nuisance to the Haskell specification, implementation, and (occasionally) programmer.

Choice 9a (Haskell): the context in a class-member type signature cannot mention the class type variable; in addition, it is subject to the same rules as any other type signature.

Choice 9b: the type signature for a class-member is subject to the same rules as any other type signature.

⁹ Recall that matching a constraint against an instance declaration is a one-way unification: we may instantiate type variables from the instance head, but not those from the constraint.

5 Other avenues

While writing this paper, a number of other extensions to Haskell's type-class system were suggested to us that seem to raise considerable technical difficulties. We enumerate them in this section, identifying their difficulties.

5.1 Anonymous type synonyms

When exposed to multi-parameter type classes and in particular higher order type variables, programmers often seek a more expressive type language. For example, suppose we have the following two classes Foo and Bar:

```
class Foo k1 where f :: k1 a -> a
class Bar k2 where g :: k2 b -> b
```

and a concrete binary type constructor

```
data Baz a b = ...
```

Then we can easily write an instance declaration that declares (Bar a) to be a functor, thus:

```
instance Functor (Baz a) where
```

```
map = ...
```

But suppose Baz is really a functor in its *first* argument. Then we really want to say is:

```
instance Functor (Zab b) where
```

```
map = ...
```

However, Haskell prohibits partially-applied type synonyms, and for a very good reason: a partially-applied type synonym is, in effect, a lambda abstraction at the type level, and that takes us immediately into the realm of higher-order unification, and minimises the likelihood of a decidable type system (Jones [1995a, Section 4.2]). It might be possible to incorporate some form of higher-order unification (e.g. along the lines of Miller [1991]) but it would be a substantial new complication to an already sophisticated type system.

5.2 Relaxed superclass contexts

One of our ground rules in this paper is that the type variables in the context of a class declaration must be a subset of the type variables in the class head. This rules out declarations like:

```
class Monad (m s) => StateMonad m where
  get :: m s
  set :: s -> m s ()
```

The idea here is that the context indicates that `m s` should be a monad for any type `s`. Rewriting this definition by overloading on the state as well

```
class Monad (m s) => StateMonad m s where
  get :: m s
  set :: s -> m s ()
```

is not satisfactory as it forces us to pass several dictionaries, say (StateMonad State Int, StateMonad State Bool) where they are really the same. What we really want is to use universal quantification:

```
class (forall s. Monad (m s))
=> StateMonad m where
  get :: m s
  set :: s -> m s ()
```

but that means that the type system would have to handle constraints with universal quantification — a substantial complication.

Another ground rule in this paper is the restriction to cyclic superclass hierarchies. Gofor puts no restriction on the form of predicates that may appear in superclass contexts, in particular it allows mutually recursive class hierarchies. For example, the Iso class example of Section 2.3 can be written in a more elegant way if we allow recursive classes:

```
class Iso a b => Iso a b where iso :: a -> b
```

The superclass constraint ensures that when a type `a` is isomorphic to `b`, then type `b` is isomorphic to `a`. Needless to say that such class declarations easily give lead to an undecidable type system.

5.3 Controlling the scope of instances

One sometimes wishes that it was possible to have more than one instance declaration for the *same* instance type. program one might like to have an instance declaration

```
instance Ord T where { (<) = lessThan }
```

and elsewhere one might like

```
instance Ord T where { (<.) = greaterThan }
```

As evidence for this, notice that several Haskell standard library functions (such as `sortBy`) take an explicit comparison operator as an argument, reflecting the fact that the Ord instance for the data type involved might not be the ordering you want for the sort. Having multiple instance declarations for the same type is, however, fraught with the risk of losing coherence; at the very least it involves strict control over which instance declarations are visible where. It is far from obvious that controlling the scope of instances is the right way to tackle this problem — functors, as in ML, look more appropriate.

5.4 Relaxed type signature contexts

In programming with type classes it is often the case that we end up with an ambiguous type while we know that in fact it is harmless. For example, knowing all instance declarations in the program, we might be sure that the ambiguous example of Section 2.3 is safe value, irrespective of the choice for `b`. Is it possible to modify the type system to deal with such cases?

Sometimes a type system is so finely balanced that virtually any extension destroys some of its more desirable properties. Haskell's type class system turns out not to have the property - there seems to be sensible extensions that gain expressiveness without involving major new complications. We have tried to summarise the design choices in a fairly unbiased manner, but it is time to nail our colours to the mast. The following set of design choices seems to define an upward-compatible extension of Haskell without losing anything important:

- Permit multi-parameter type classes.
- Permit arbitrary constraints in types and type signatures (Choice 1b).
- Use the (*inst*) context-reduction rule only when forced by a type signature, or when the constraint is tautological (Choice 2d). Choice 2e is also viable.
- Prohibit overlapping instance declarations (Choice 3a).
- Permit arbitrary instance types in the head of an instance declaration, except that at least one must not be a type variable (Choice 4c).
- Permit repeated type variables in the head of an instance declaration (Choice 5a).
- Restrict the context of an instance declaration to mention type variables only (Choice 6b).
- No limitations on superclass contexts (Choice 7b).
- Prohibit improvement (Choice 8a).
- Permit the class variable(s) to be constrained in class member type signatures (Choice 9b).

Our hope is that this paper will provoke some well-informed debate about possible extensions to Haskell's type classes. We particularly seek a wider range of examples to illustrate and motivate the various extensions discussed here.

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References

- K Chen, P Hudak & M Odersky [June 1992], "Parametric type classes," in *ACM Symposium on Lisp and Functional Programming*, Snowbird, ACM.
- C Elliott & P Hudak [June 1997], "Functional reactive animation," in *Proc International Conference on Functional Programming*, Amsterdam, ACM.
- P Hudak, SL Peyton Jones, PL Wadler, Arvind, B Boutel, J Fairbairn, J Fasel, M Guzman, K Hammond, J Hughes, T Johnson, R Kieburtz, RS Nikhil, W Partain & J Peterson [May 1992], "Report on the functional programming language Haskell, Version 1.2," *SIGPLAN Notices* 27.
- MP Jones [Jan 1995a], "A system of constructor classes: overloading and implicit higher-order polymorphism," *Journal of Functional Programming* 5, 1-36.
- MP Jones [June 1995b], "Simplifying and improving qualified types," in *Proc Functional Programming Languages and Computer Architecture*, La Jolla, ACM.
- MP Jones [May 1994], "The implementation of the Gopher functional programming system," YALEU/DCS/RR-1030, Department of Computer Science, Yale University.
- MP Jones [May 1995], "Functional programming with overloading and higher-order polymorphism," in *First International Spring School on Advanced Functional Programming Techniques*, Bastad, Sweden, Springer-Verlag LNCS 925.
- MP Jones [Nov 1994], *Qualified types: theory and practice*, Cambridge University Press.
- S Kaes [Jan 1988], "Parametric overloading in polymorphic programming languages," in *15th ACM Symposium on Principles of Programming Languages*, ACM, 131-144.
- J Launchbury & SL Peyton Jones [Dec 1995], "State in Haskell," *Lisp and Symbolic Computation* 8, 293-342.
- S Liang, P Hudak & M Jones [Jan 1995], "Monad transformers and modular interpreters," in *22nd ACM Symposium on Principles of Programming Languages*, San Francisco, ACM.
- D Miller [1991], "A logic programming language with lambda abstraction, function variables, and simple unification," *Journal of Logic and Computation* 1.
- M Odersky, PL Wadler & M Wehr [June 1995], "A second look at overloading," in *Proc Functional Programming Languages and Computer Architecture*, La Jolla, ACM.

- C Okasaki [Sept 1996], "Purely functional data structures,"
 PhD thesis, CMU-CS-96-177, Department of Com-
 puter Science, Carnegie Mellon University.
- SL Peyton Jones [Sept 1996], "Bulk types with class,"
 in *Electronic proceedings of the 1996 Glas-
 gow Functional Programming Workshop* ([http://www.dcs.gla.ac.uk/ftp/workshops/fp96/-
 Proceedings96.html](http://www.dcs.gla.ac.uk/ftp/workshops/fp96/-

 Proceedings96.html)).
- SL Peyton Jones, AJ Gordon & SO Finne [Jan 1996], "Con-
 current Haskell," in *23rd ACM Symposium on
 Principles of Programming Languages, St Peters-
 burg Beach, Florida, ACM, 295-308.*
- PL Wadler & S Blot [Jan 1989], "How to make ad-hoc poly-
 morphism less ad hoc," in *Proc 16th ACM Sym-
 posium on Principles of Programming Languages,*
 Austin, Texas, ACM.

Polyomorphic Extensible Records for Haskell

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Abstract

This paper describes an extension of Haskell that supports extensible records, with a full complement of polyomorphic operations. It is a practical system which can be understood and implemented as a natural extension of Haskell. The proposed extensions have been implemented as part of the Hugs development system, and seem to work well in practice.

1 Introduction

Datatypes play an important role in all but the most trivial of programming tasks. For example, consider a program specification which requires that a selection of geometric shapes be transformed in variety of different ways. It is reasonable, even with only this informal description, to imagine a collection of new datatypes, one for each geometric shape, each of which may have a number of associated attributes. But how are such types represented in a program? In functional languages like Haskell [19], and Standard ML [15] products provide support for defining datatypes, allowing a selection of data items to be grouped together. For example, a datatype representing the geometric shape point, might be represented by the following Haskell definition:

```
data Point = MkPoint Int Int.
```

Although adequate, this definition is not particularly easy to work with in practice. For example, it is easy to confuse fields when they are accessed by position within a product. To avoid these problems, the programming languages Haskell and Standard ML allow components of products to be identified using names drawn from some set of labels. Haskell 1.3 provides support for labelled products by allowing a datatype declaration to include field labels for components of the datatype. For example, the

```
type Point = Rec { x :: Int, y :: Int }.
```

Alternatively, Standard ML supports a more general notion of record types, which considers labelled products as separate entities from datatype declarations. In this setting, our *Point* example can be reformulated as¹:

```
data Point = MkPoint { x :: Int, y :: Int }.
```

Point type described above might be defined more attractively as:

Although Standard ML does not require that we pre-define a type synonym for *Point*, in practice, it does provide a useful way of documenting one's intentions. Both Haskell and Standard ML provide mechanisms allowing field names to be used in the construction and selection of record components without concern for the overall structure of the datatype. For example, Haskell ensures that, for each new label, a function working as a selector for that component is introduced at the top-level. Unfortunately, this has the undesirable side effect of forcing any two datatypes defined within the same scope, to use mutually exclusive field names. For example, returning again to the notion of geometric shapes, a datatype definition for circles including components *x*, *y*, and *r* representative of the circle's centre point and radius respectively, might be defined as:

```
data Circle = MkCircle { x :: Int, y :: Int, r :: Int }.
```

However, this definition is not valid if defined in the same scope as the *Point* shape described above. Moreover, datatypes defined in separate modules sharing common field names may only be used in the same namespace with careful use of qualified names. Standard ML avoids imposing similar restrictions on record fields, by requiring that the type of a record *r* is uniquely determined at compile-time. In effect, each different record

¹To emphasize the notion of record types, we choose to incorporate a record constructor, *Rec*, where in fact the actual Standard ML definition is: `type Point = { x :: Int, y :: Int }.`

type that includes an l field comes with its own method for extracting the value of that field. By requiring that the record type can be determined during type checking, the overloading that results from using the same notation for each of these operations is easily resolved. An unfortunate consequence of the restrictions imposed on record types by both the Haskell and Standard ML type systems is that operations provided for manipulating records are less flexible than might be expected. For example, consider operations to extract the centre point of a given shape. We might reasonably expect that polymorphism would provide the ability to define a single definition for all shapes:

$$\text{centre shape} = (\text{shape} . x, \text{shape} . y),$$

where $(-x)$ denotes selection of the field x from some arbitrary record. However, although both Haskell and Standard ML provide support for polymorphic definitions, no support is provided for the analogous idea of polymorphism over fields, which allows unimportant labels to be ranged over by a single variable. It is the requirement that record types be completely determined at compile-time—enforced by the application of constructors in Haskell, and by user specified type annotations in Standard ML—that limit operations over records to monomorphic type. A further weakness of the Haskell and Standard ML record systems is that no support is provided for *extensibility*; there are no general operators for adding and removing fields in a record value, for example. The following definition, which is not legal in either Haskell or Standard ML, shows how extensibility might be applied to allow an additional colour field to be incorporated into arbitrary shape values:

$$\text{colour } c \text{ shape} = (\text{colour} = c | \text{shape}),$$

where the operator $(\text{colour} = | -)$ denotes the extension of an arbitrary record with a new field *colour*.

1.1 This paper

This paper presents an alternative proposal for records in Haskell², by combining ideas that have been used in previous work to develop a practical type system. In particular, it supports extensible records, with a full complement of polymorphic operations. For example, the point and circle shapes described above can be reformulated as:

$$\begin{aligned} \text{type Shape } r &= \text{Rec } \{ x :: \text{Int}, y :: \text{Int} | r \} \\ \text{type Circle} &= \text{Shape } \{ \text{rad} :: \text{Int} \}. \end{aligned}$$

²The record system discussed in this paper would be equally suitable for an extension of Standard ML. However, the type system is based on the notion of qualified types, which is the core type system of Haskell, and as such, Haskell seems an obvious choice.

Here record type extension, denoted by $\{ l :: - | - \}$, provides us with the ability to define *Circle* as an extension of the type *Shape* which includes at least the fields x and y ; i.e., a value of type *Shape* is at least a value of type *Point* introduced above. Intuitively, a value of type *Circle* contains all the fields of a *Shape*, plus an extra component *rad*. In fact, we might have done equally well to define *Circle* as:

$$\text{type Circle} = \text{Rec } \{ x :: \text{Int}, y :: \text{Int}, r :: \text{Int} \}.$$

The combination of extensibility, and the ability to define polymorphic operations over records provides us with the functionality to define, and type correctly, the definition of *centre* described above:

$$\begin{aligned} \text{centre} &:: \text{Rec } \{ x :: \text{Int}, y :: \text{Int} | r \} \rightarrow (\text{Int}, \text{Int}) \\ \text{centre shape} &= (\text{shape} . x, \text{shape} . y) \end{aligned}$$

Note, that unimportant fields (e.g., the radius component of a circle) are bound to the variable r .

This paper provides an informal presentation of extensible records for Haskell and retrains from in depth discussion of related record calculi. In particular we do not consider proposals for extending Standard ML with similar record operations, for example Rémy [21, 22] and Othor [18]. For an in depth formal treatment of the record system proposed in this paper, including a discussion of related work, the interested reader might look at Gaster and Jones' paper introducing a record and variant calculi for qualified types [6]. We conclude this section by outlining the main subjects covered in the remaining parts of this paper:

- Section 2 provides an informal overview of our proposal for extensible records in Haskell. A number of basic record operations are considered, which are natural generalizations of operators that are already present in Haskell.
- Section 3 describes an implementation for extensible records. Analogous to the standard notion of class constraints representing implicit dictionary parameters, field constraints are considered as evidence for offsets into a given record.
- Section 4 considers a number of pragmatic issues concerning the integration of extensible records into Haskell. In particular, any serious proposal extending Haskell with new primitive datatypes, must consider the general framework of deriving instances for standard classes (e.g., equality), and must address questions of syntax, and pattern matching.
- Section 5 concludes, summarizing some possibilities for future work.

2 Basic record operations

Record types are defined by application of the constructor *Rec* to well-formed rows, which are themselves constructed by extension, starting from the empty row, $\{\}$. A row may be thought of as partial function from labels to simple types. It is convenient to introduce abbreviations for rows obtained in this way:

$$\{l_1::\tau_1, \dots, l_n::\tau_n\} = \{l_1::\tau_1 | \dots | l_n::\tau_n\} \\ \{l_1::\tau_1, \dots, l_n::\tau_n\} = \{l_1::\tau_1, \dots, l_n::\tau_n\} \{\}$$

Note, however, that we treat rows, and hence record types, as equals if they include the same fields, regardless of the order in which those fields are listed. Intuitively, a record of type $Rec\ \{l :: \alpha \mid r\}$ is like a pair whose first component is a value of type α , and whose second component is a record of type $Rec\ r$. This motivation closely to the projection and pairing functions of Haskell product types. There is, however, one complication; we do not allow repeated uses of any label within a particular row, so the expression $\{l :: \alpha \mid r\}$ is only valid if l does not appear in r . This is reflected by prefixing each of the types below with a predicate $(r \setminus l)$, pronounced “ r lacks l ”:

- Selection: to extract the value of a field l :
 $(-.\!l) :: (r \setminus l) \Rightarrow Rec\ \{l :: \alpha \mid r\} \rightarrow \alpha$
- Restriction: to remove a field labelled l :
 $(-\!l) :: (r \setminus l) \Rightarrow Rec\ \{l :: \alpha \mid r\} \rightarrow Rec\ r$
- Extension: to add a field l to an existing record:
 $(l = -\!l) :: (r \setminus l) \Rightarrow \alpha \rightarrow Rec\ r \rightarrow Rec\ \{l :: \alpha \mid r\}$

A predicate of the form $(r \setminus l)$ prevents a record r being extended with a field already present, but no analogous operation is provided at the level of types. However, although record types containing multiple occurrences of the same label are legal (e.g., $Rec\ \{l :: Bool, l :: Int\}$ is a valid type), they are uninhabited³, and as such, it is impossible to construct proper values with the appropriate type. In practice a compiler may incorporate static checks to avoid record types with multiple labels within module boundaries. For example, consider the following type definitions:

$$type\ Foo\ r = Rec\ \{l :: Int \mid r\} \\ type\ Foo' = Foo\ \{l :: Bool\}$$

³The primitive operation for record extension insures, by means of a predicate $r \setminus l$, that a record is only ever extended with a field not already present.

Expanding Foo' gives the type expression

$$Rec\ \{l :: Bool, l :: Int\},$$

which can be flagged as an error at compile-time.

We can use the basic operations described above to implement a record update operation which, unlike datatypes with labelled fields, does not restrict the type of the updated field:

$$(l := -\!l) :: (r \setminus l) \Rightarrow \alpha \rightarrow Rec\ \{l :: \beta \mid r\} \\ \rightarrow Rec\ \{l :: \alpha \mid r\} \\ (l := x \mid r) = (l := x \mid r - l)$$

As a concrete example of these operations, and highlighting the use of extensibility, consider a hierarchy of algebraic structures in which monoids (structures with a set and an associative binary operation) form the base of the hierarchy, and group and ring structures are defined as extensions of monoids and groups, respectively. A group supports all operations of a monoid plus an inverse, and a ring supports all operations of a group plus some of its own. Given, an appropriate implementation of this hierarchy, a user might reasonably expect to define operations, requiring only the functionality of monoids, over all algebraic structures. Figure 1 provides an implementation of this hierarchy in terms of extensible records, accompanied by sample implementations, for the integers.

type Monoid $v\ r = Rec\ \{plus :: v \rightarrow v \rightarrow v, id :: v \mid r\}$	type Monoid $v\ r = Monoid\ v\ \{inv :: v \rightarrow v \mid r\}$	type Ring $v\ r = Group\ v\ \{null :: v \rightarrow v \rightarrow v, one :: v \mid r\}$	Monoid	Monoid	Monoid	Group	Group	Ring	Ring
$Rec\ \{plus :: v \rightarrow v \rightarrow v, id :: v \mid r\}$	$Monoid\ v\ \{inv :: v \rightarrow v \mid r\}$	$Group\ v\ \{null :: v \rightarrow v \rightarrow v, one :: v \mid r\}$	$Monoid\ Int\ \{plus = (+), id = 0\}$	$Group\ Int\ \{inv = negate \mid Monoid\}$	$Ring\ Int\ \{null = (*), one = 1 \mid Group\}$				

Figure 1: Example algebraic hierarchy

The standard list function *sum*, for computing the sum of a list, can now be recast in terms of any monoid:

$$sum\ Monoid\ \alpha\ r \rightarrow \alpha \quad :: \quad Monoid\ \alpha\ r \rightarrow \alpha \quad [foldr\ (mon.plus)\ (mon.id)\ sum\ mon =]$$

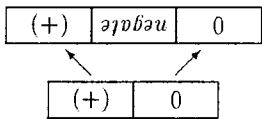
operator, $(l = |-)$, can be implemented by a function $\lambda i.\lambda v.\lambda r.pert\ i\ v\ r$, using the extra parameter i to supply the offset at which the value v is to be inserted into the record r . For example, the expression:

```
(inv = negate | iMonoid)
```

can be implemented by compiling it to

```
(\i.\v.\r.pert\ i\ v\ r) 1 negate iMonoid,
```

assuming a lexicographical ordering on labels. The resulting expression, $pert\ 1\ negate\ iMonoid$, can be implemented by simple copying procedures, allowing the correct insertion of the value $negate$. This process is captured diagrammatically by the following diagram:



Note, that all fields with labels considered less than the label being inserted, remain in the same position in the array, while all fields following the inserted field are shifted up one position. Record restriction can be implemented in a similar fashion, where instead of larger field labels being shifted up one position they are shifted down one.

Of course, there are run-time overheads in calculating and passing offset values as extra parameters. However, an attractive feature of our system is that these costs are only incurred when the extra flexibility of record extension and polymorphic selection is required. Operations like record extension and restriction will, in general, be implemented by copying. Optimizations can be used to combine multiple extensions or restrictions of records, avoiding unnecessary allocation and initialization of intermediate values. For example, a compiler can generate code that will allocate and initialize the storage for a record $(x = 1, y = 2, z = 3)$ in a single step, rather than a sequence of three individual allocations and extensions as a naive interpretation might suggest.

The typechecker gathers and simplifies the predicates generated by each use of an operator on records. For example, if $iMonoid$ is a value of type $Monoid\ Int$, then an expression like $iMonoid\ id$ will generate a single constraint, $\{plus :: Int\ id$. Predicates like this, involving rows whose structure is known at compile-time, are easily discharged by calculating the appropriate offset value. Obviously, a compiler can use this information to produce efficient code by inlining and specializing the selector function, $(-id)$.

It is possible that our more general treatment of record operations could result in compiled programs

Here, r ranges over rows containing zero or more fields, which in the case when the function sum is applied to $iGroup$, r is bound to the single field $negate$. Thus extensibility captures a form of sub-typing that is also present, although in a slightly different form, in the Haskell class system. However, we believe that this notion of sub-typing is present in a number of different programming situations, many of which are more suited to extensibility than they are to obscure encodings using the class mechanism.

Extensibility provides a simple form of inheritance, more commonly found in object-oriented languages [23, 2, 1]. Hughes and Spard [7], have shown that the Haskell class system provides an alternative form of inheritance, which can be utilized to encode object-oriented features. It remains to be seen whether records with extensibility will provide a practical platform for incorporating object-oriented features into Haskell.

3 Record implementation

This section explains how the data structures and operations described in the previous section can be implemented. We focus on the implementation of record extension, $(l = |-)$, which, aside from record selection, is probably the most frequently used basic operation. A naive approach would be to represent a record by an association list, pairing labels with values. This would allow simple implementations for each of the basic operations, with the type system providing a guarantee that the same field would never appear more than once in a given record. A major disadvantage is that it does not allow constant time access to record components.

To avoid these problems, we will assume instead that a record value is represented by a contiguous block of memory that contains a value for each individual field. To select a particular component $r.l$ from a record r , we need to know the offset of the l field in the block of memory representing r . Languages without polymorphic selection will usually allow an expression of the form $r.l$ if the offset value, and hence the structure or even the full type of r , as in Haskell, is known at compile-time.

However, it is not actually necessary to know the position of every field at compile-time; instead, we can treat unknown offsets as implicit parameters whose values will be supplied at run-time when the full types of the records concerned are known. This is essentially the compilation method that was used by O'Hori [18], and also suggested, independently, by Jones [8]. Assuming records are implemented as arrays of equally sized cells, in which record fields are stored consistently with respect to some total ordering on labels, the extension

Unquestionably, choosing an appropriate syntax plays an important role in the success or failure of programming language features. For example, Haskell allows pattern matching on the left hand side of function bindings, which in turn provides a convenient mechanism for describing inductive definitions. If however, pattern matching was supported only within the case construct, then inductive definitions may not seem as attractive. Section 2 introduced a syntax for record types and operations, which overlapped with that of Haskell. For example, record selection was written using the symbol (\cdot), which is already used for function composition in Haskell. The fact that we use the symbols $\{$ and $\}$, which are not defined by Haskell's lexical syntax, complicates matters even further.

Any discussion of syntax for extensible records in Haskell, must consider whether records as described by the Haskell 1.3 report are to be retained. If not retained, then the syntax for record types can be simply that of Section 2, replacing the symbols $\{$ and $\}$ with $\{$ and $\}$ respectively. As the system presented in this paper supports the record operations of Haskell, we believe that it is not unreasonable to consider replacing one by the other.

We now turn our attention to the question of syntax for record values. Our main concern is that the syntax of Section 2 introduces ambiguities when considered with respect to Haskell's syntax. Unfortunately, although record extension integrates smoothly, this is not the case for either record selection or restriction. In practice we have found only a few applications for record restriction, and in such cases pattern matching over records has proven adequate. In contrast, record selection appears in all but the most trivial of record applications, and although pattern matching provides an alternative, we believe that this operation must be supported using a convenient notation.

Record selection in Standard ML [15] is represented by the appropriate label prefixed by the symbol $\#$. Thus selection of the field l of a record r is denoted by the expression $\#l r$. However, having experimented with this notation, we found that important program details were often hard to visualize. With this in mind, we strongly believe that (\cdot) is the correct notation for record selection. This leaves us with the important question of what to do about function composition, which is denoted by the symbol (\cdot) in current versions of Haskell. It may come as a surprise to the reader that, in fact, we propose that function composition be represented by the symbol $\#$, even though we felt it to be inappropriate for record selection. Moreover, since function composition is in fact an instance of the Haskell

that are littered with unwanted offset parameters; experience with our prototype implementation will help to substantiate or dismiss these concerns. In any case, there are simple steps that can be taken to avoid such problems. For example, a compiler might reject any definition with an inferred type containing predicates, unless an explicit type signature has been given to signal the programmer's acceptance. This is closely related to the *monomorphism restriction* in Haskell and to proposals for a *value restriction* in Standard ML [24, 13].

4 Pragmatic Issues

Previous sections highlighted a number of shortcomings with the current solution for records in Haskell, and proposed a system of polymorphic extensible records, naturally extending the Haskell type system. However, hitherto we have avoided considering the more pragmatic issues, which often arise with proposed extensions to non-trivial languages, such as Haskell. In this section we consider three particularly important practical concerns for extensible records in Haskell. Section 4.1 considers the question of pattern matching over records. Section 4.2 highlights the difficulty in selecting a suitable syntax. Section 4.3 presents extensions of the Haskell class mechanism, to allow for derived instances of equality and text operations over records.

4.1 Pattern matching

As with other datatypes in Haskell, pattern matching is often a natural way to extract the components of a record. For example, considering again the algebraic hierarchy of Section 2, pattern matching provides an alternative definition for the function *sum*:

$$\text{sum} \quad \text{::} \quad \text{Monoid } \alpha \Rightarrow \alpha \rightarrow \alpha$$

$$\text{sum } (dls = d, dl = l) r = \text{foldr } d \ l \ r$$

Intuitively an expression of the form *sum* e is evaluated from left to right, first evaluating the pattern bindings for d and l , and then binding all other components to the pattern r . More generally we can explain the semantics of pattern matching over records using a translation of the form:

$$\lambda(l = d \mid r) \rightarrow e \triangleq \lambda x \rightarrow \text{case } x \text{ of } d \rightarrow l \text{ of } r \rightarrow e.$$

Note that, although we propose that the source level use of record restriction be restricted to patterns only (see Section 4.2), our implementation of pattern matching requires record restriction as a primitive notion. However, such uses do not introduce any new syntactical problems.

class *Func*or *f* where

```
(#) :: (α -> β) -> (f α -> f β)
```

Function composition is defined simply as an instance

of this class:

```
instance Funcor (→) α where
  f#(g) x = f (g x)
```

Fortunately, associativity for function composition is preserved. To see this, recall that the following equation is satisfied by any functor [12]:

$$f \# (g \# h) = f \# (g \# h)$$

for which *f*, *g* and *h* are of the appropriate types. Instantiating the different uses of (#) to function composition, of the appropriate types, gives the equality⁴:

$$(f \cdot g) \cdot h = f \cdot (g \cdot h)$$

which is precisely the required associativity law.

Figure 2 contains our proposed extensions for the Haskell grammar, which itself appears in appendix B of the Haskell report [19].

A more long term perspective for adopting an alternative record proposal for Haskell, might involve considering tuples of type (τ_1, \dots, τ_n) to be shorthand for records of type $\text{Rec } \# \{ \tau_1, \dots, \tau_n \}$. A similar relationship between tuples and records has been adopted by Standard ML [15], and seems to provide a number of practical benefits, not least a general mechanism for selecting arbitrary components of tuples.

4.3 Records and the Haskell class system

Often, the design and implementation of a new datatype requires more than just specifying the datatype definition itself. For example, one must ask questions such as: Is equality defined over elements of the new datatype? Are elements of this type printable? And so on. Although many of these questions will be related to specific applications, there is a class of operations that arise for almost all datatypes (e.g., equality). To ease the programming burden, Haskell provides a number of predefined type classes for operations such as equality and printing, for which instances can be derived automatically by the compiler. This section considers how an implementation might automatically derive instances of the *Eq* and *Show* classes over records. We return briefly to denoting function composition as (\cdot), in order to help the discussion.

An obvious first attempt at defining equality over records might involve having the compiler generate instance declarations of the form:

```
instance (Eq r, Eq α) => (Eq (Rec # α | r#)) where
  r == r' = (r.l == r'.l) && (r - l == r' - l)
```

for each record extension with a field *l*. However, even if we overlook the fact that Haskell does not support contexts of the form shown here, this does not give a well-defined notion of equality. To see this consider the expression:

$$(x = 10, y = 20, z = 30),$$

where \perp is a diverging term of type *Int*. Evaluating this expression from left to right results in the boolean value *False*. However, we consider rows equal modulo reordering of fields, thus applying commutativity and evaluating from left to right gives \perp for the above equality. Thus if we are not careful when deriving equality over records, then it is possible that different implementations may produce differing results. The problem lies in the fact that rows, and thus records, are considered equal modulo reordering of fields.

The clue to resolving this problem lies in Section 3, where the well-formedness of record compilation was guaranteed by considering a total ordering on labels. Intuitively, equality over records is well-defined if corresponding pairs of fields are compared in precisely the order determined by their labels in the record type that we are concerned with. Operationally, one can think of record equality as: given any two records of the same type, construct an ordered list of pairs, in which the first element of each pair is the string for a particular label and the second is a (delayed) boolean test of equality for the values associated with a given label. The following class definition captures this notion of equality over records:

```
class EqRec r where
  eqRec :: Rec r -> Rec r -> (String, Bool)
```

To ensure that the definition of equality over records is well-defined, an implementation must guarantee that instances of this class can only be generated internally, on application of the extension operator. The instance for the empty row can be predefined, in a suitable library, as:

```
instance EqRec [] where
  eqRec [] = []
```

Now, providing that suitable implementations are constructed on each application of record extension, we

- *First class polymorphism and extensible records:* Recent work by Lauter and Odersky [17], Jones [11], and Garriague and Remy [5] has shown that a type system based upon let-polymorphism [14, 3, 4] can be extended to allow polymorphic values as first class citizens. A common theme in this work is the requirement that hints are provided to the type inference system (for example, polymorphic values can be constructed by application of constructor functions). It is our belief that such hints may be provided by the construction and deconstruction of record values and on going work is showing promising results.
- *First class modules for Haskell:* It has long been realized that the Standard ML module system provides a range of software engineering benefits over that of the Haskell module system. It is to this end, that we are interested in unifying and combining the record system described in this paper, with Jones' [10] mechanism for modules using parameterized signatures, with the long term objective of incorporating first class modules into Haskell.
- *A new approach to datatypes:* Gaster and Jones [6] have shown that the type system providing support for the operations introduced in Section 2 not only supports extensibility over records, but also provides this functionality for variants. To this

We have described a natural extension to Haskell, that is flexible enough to allow polymorphic extensible records. This system generalizes the current Haskell and Standard ML record systems, allowing polymorphic operations over records and extensibility. A prototype implementation has been incorporated into Hugs, an implementation of Haskell 1.3 [9]. Our experience to date shows that the implementation works well in practice. There are a number of areas for further work:

5 Conclusion

Derivable instances may be defined similarly for the classes *Ord* and *Show*. For example, Figure 3 contains an implementation for showing record values⁵. Analogous with the function *eqRecRow*, described above, the function *showRecRow* generates an ordered list of pairs for a given record. The second component of each pair represents the showable value associated with a given label *l*.

```
instance EqRecRow r => Eq (Rec r) where
  x == y = all (map snd (eqRecRow x y))
```

can safely define a single, general, instance for equality over records:

Figure 2: Proposed syntax for extensible records in Haskell

label	→	varid	(field names)
rowvar	→	lvar	(row variables)
row	→	{label ₁ :: type ₁ , ..., label _n :: type _n row}	(row variables)
atype	→	Rec row	(record type)
fexp	→	[fexp]dexp	(function application)
dexp	→	dexp.label	(record selection)
exp	→	(label ₁ = exp ₁ , ..., label _n = exp _n) (label ₁ = exp ₁ , ..., label _n = exp _n exp)	(n ≥ 0) (n ≥ 1)
apal	→	(label ₁ = pal ₁ , ..., label _n = pal _n) (label ₁ = pal ₁ , ..., label _n = pal _n pal)	(n ≥ 0) (n ≥ 1)

⁵Following the discussion of Section 4.2 the composition of functions is represented by (#) :: (α → β) → (γ → α) → γ → β.

Notes in Computer Science, pages 51-67. Springer-Verlag, 1984. Full version in *Information and Computation* 76(2/3):138-164, 1988.

[3] L. Damas and R. Milner. Principal type schemes for functional programs. In *Proceedings of the 9th ACM Symposium on Principles of Programming Languages*, pages 207-212, 1982.

[4] L. M. Damas. *Type Assignment in Programming Languages*. PhD thesis, University of Edinburgh, April 1985. Technical report CST-33-85.

[5] J. Garrigue and D. Rémy. Extending ML with semi-explicit higher-order polymorphism. In *International Symposium on Theoretical Aspects of Computer Software*, September 1997.

[6] B. R. Gaster and M. P. Jones. A polymorphic type system for extensible records and variants. Technical Report NOTTCS-TR-96-3, Computer Science, University of Nottingham, November 1996.

[7] J. Hughes and J. Sparrud. Haskell++: An object-oriented extension of Haskell. In *Proceedings of Haskell Workshop, La Jolla, California, YALE Research Report DCS/RR-1075*, 1995.

[8] M. P. Jones. *Qualified Types Theory and Practice*. Distinguished Dissertations in Computer Science. Cambridge University Press, 1994.

[9] M. P. Jones. The Hugs 1.3 distribution. Available from the University of Nottingham: <http://www.cs.nott.ac.uk/Department/Staff/mpj/>. August 1996.

[10] M. P. Jones. Using parameterized signatures to express module structure. In *Proceedings of the 3rd Symposium on Principles of Programming Languages*, pages 68-78. ACM, January 1996.

[11] M. P. Jones. First-class polymorphism with type inference. In *Proceedings of the 24th Symposium on Principles of Programming Languages*, pages 483-496. ACM, January 1997.

[12] S. M. Lane. *Categories for the Working Mathematician*. Graduate Texts in Mathematics. Springer-Verlag, 1972.

[13] X. Leroy. Polymorphism by name for references and continuations. In *Principles of Programming Languages*, pages 220-231. ACM press, 1993.

[14] R. Milner. A theory of type polymorphism in programming. *Journal of Computer and System Sciences*, 17:348-375, August 1978.

[1] T. Budd. *An Introduction to Object-Oriented Programming*. Addison-Wesley, Reading, MA, 1991.

[2] L. Cardelli. A semantics of multiple inheritance. In G. Kahn, D. MacQueen, and G. Plotkin, editors, *Semantics of Data Types*, volume 173 of *Lecture Notes in Computer Science*. Springer-Verlag, 1989.

References

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end, we are interested in developing the ideas in this paper into a general framework for extensible datatypes in Haskell.

• *Object-oriented programming in Haskell*: Section 2 noted that extensibility is closely related to inheritance found in languages based on an object-oriented methodology. A general notion of extensibility is captured through our use of rows, which potentially may be suitable for object-oriented extensions of Haskell. For example, a constructor row of methods [16, 20].

Figure 3: Functions to "show" record values

```

Instance ShowRec r => Show (Rec r) where
  showRec d = showFields#showRecRow

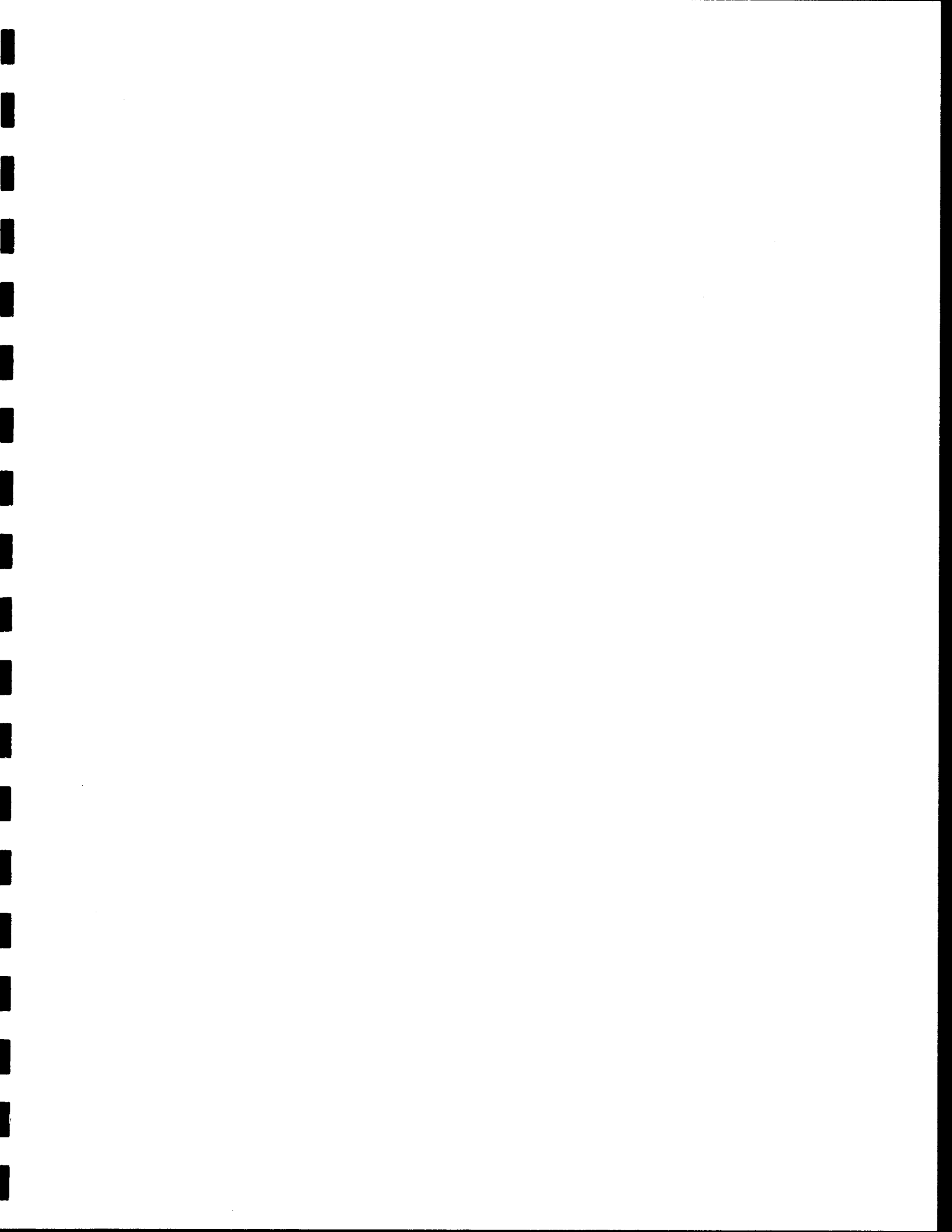
showFields :: [(String, ShowS)] -> ShowS
showFields [] = showString "()"
showFields xs = showChar '('
# foldr1 comma (map fld xs)
# showChar ')'

fld (s, v) = a#showString ", " # b
          = showString s#showChar ' = #v

class ShowRecRow r where
  showRecRow :: Rec r -> [(String, ShowS)]
Instance ShowRecRow {} where
  showRecRow = []

```

- [15] R. Milner, M. Tofte, and R. Harper. *The definition of Standard ML*. The MIT Press, 1990.
- [16] J. C. Mitchell, F. Honsell, and K. Fisher. A lambda calculus of objects and method specialization. In *1993 IEEE Symposium on Logic in Computer Science*, June 1993.
- [17] M. Odersky and K. Läufer. Putting type annotations to work. In *Proceedings of the 24th Symposium on Principles of Programming Languages*, pages 65-67. ACM, January 1996.
- [18] A. Ohori. A polymorphic record calculus and its compilation. *ACM Transactions on Programming Languages and Systems*, 17(6):844-895, Nov. 1995. Preliminary version in *Proceedings of ACM Symposium on Principles of Programming Languages*, 1992, under the title, A compilation method for ML-style polymorphic record calculi.
- [19] J. Peterson and K. Hammond. Report on the Programming Language Haskell, A Non-strict, Purely Functional Language (Version 1.3). Technical Report YALEU/DCS/RR-1106, Yale University, Department of Computer Science, May 1996.
- [20] B. C. Pierce and D. N. Turner. Simple type-theoretic foundations for object-oriented programming. *Journal of Functional Programming*, 4(2):207-247, Apr. 1994. A preliminary version appeared in *Principles of Programming Languages*, 1993, and as University of Edinburgh technical report ECS-LFCS-92-225, under the title "Object-Oriented Programming Without Recursive Types".
- [21] D. Rémy. Projective ML. In *1992 ACM Conference on Lisp and Functional Programming*, pages 66-75, New-York, 1992. ACM press.
- [22] D. Rémy. Type inference for records in a natural extension of ML. In C. A. Gunter and J. C. Mitchell, editors, *Theoretical Aspects of Object-Oriented Programming: Type, Semantics, and Language Design*, Foundations of Computing Series. MIT Press, 1994. Early version appeared in Sixteenth Annual Symposium on Principles of Programming Languages, Austin, Texas, January 1989.
- [23] M. Wand. Complete type inference for simple objects. In *Proceedings of the IEEE Symposium on Logic in Computer Science*, Ithaca, NY, June 1987.
- [24] A. Wright. Simple imperative polymorphism. *Lisp and Symbolic Computation*, 8(4):343-356, December 1995.



The Design and Implementation of Mondrian

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Abstract

The Haskell dialect Mondrian is designed using the explicit philosophy of keeping things simple and consistent. Mondrian generalizes some of Haskell's (too) complex constructs, and adds a few simple new ones. This results in a small, intuitively comprehensible language with an object oriented flavor.

In this paper, we will present the design decisions we made for Mondrian. Furthermore, some of Mondrian's language constructs will be defined by translations into Haskell.

1 Introduction

In the preface of the Haskell report [13] the hope is expressed that extensions or variants of the language will appear that incorporate experimental features. The language Mondrian is such an experiment. Mondrian evolved from Haskell by deleting and combining some of Haskell's more complicated constructs and adding a few simple new ones. Unlike the language Pizza [29], which is designed as a strict superset of Java [8], the major concern in designing Mondrian has been to keep the language as basic and down to the bare essence as possible, even if this implied breaking compatibility with Haskell. We do define Mondrian by translating it into Haskell.

The hype about object-oriented programming is not without cause. Viewing the world as a collection of interacting objects is conceptually very natural. When it comes down to programming the behavior of objects in an imperative language, however, we miss the abstraction mechanisms offered by functional languages, and we are less enthusiastic. Mondrian combines algebraic data types and type classes into a naive (no real subtyping) object-oriented type system, so that it becomes possible to program in an object-oriented style within the functional paradigm. Mondrian does not pretend to be a real object-oriented language. All type-checking remains covariant and "message not understood" runtime errors are not prevented by the type checker. Fundamentally though, Haskell suffers from the very same problem.

Item in the sense that the compiler does not reject partial functions defined using pattern matching, something that is not normally perceived as a *typing* issue.

Types are significant in the programming process. Most of us share the experience that once we have the types right, the program is correct. Therefore it is a pity that in Haskell the abstraction mechanisms on the level of types fall short when compared to those on the level of expressions. On the term level we have let-expressions to name program fragments, and λ -expressions and application to parameterize over program fragments. We should be able to use these on the type level as well. Instead of Haskell's primitive mechanism of type synonyms, Mondrian has a full functional language available on the level of types, but we push the borders just a little bit to keep things as simple as possible.

If we think that it is a good idea that programmers document their code by supplying explicit type signatures for function definitions, their programming language should encourage this by providing convenient mechanisms to give type annotations. In particular, the programmer should be able to specify types of locally defined functions that are polymorphic in some type variables and monomorphic in others. Mondrian follows SML by introducing scoped type variables.

As an experiment the syntax of Mondrian modules is made consistent with that of value definitions. Identifiers that are exported must be marked as such at their declaration instead of writing them as arguments in the module heading. From a software engineering point of view this leads to more weakly coupled code. In the current situation, changing the name of an identifier requires changing a name in the export list as well. We do not consider the lack of explicit module interfaces to be a problem. In contrary, module interfaces should be generated automatically by a program browser.

At the implementation level, a novel aspect of Mondrian is the use of Pure Type Systems [10] as a typed intermediate language [24]. Instead of having three different list languages for terms, types and kinds, all of which must support similar operations, it is more convenient to have a single language that captures all levels, and allows control over the way levels can interact. A uniform framework like PTS provides an even greater degree of generality than the Glasgow Haskell Compiler backend [22], which is based on the polymorphic lambda calculus.

2 History, motivation and background

Functional programming plays an important role in the computing science curriculum at Utrecht University. For teaching, the disadvantages of functional languages such as slow speed and large memory consumption are not prohibitive, as they are for industrial usage. Moreover, the advantages of functional languages [16] such as abstraction from evaluation order (lazy evaluation), abstraction from computational patterns (higher-order functions), abstraction from type structure (polymorphism), and high code density, prove to be of great didactical value.

In the last few years we have replaced mathematical syntax by a functional language, in case Gofert [17], in a number of courses [1] including *Grammars and Parsing*, *Computer Architecture*, and *Implementations of Programming Languages*. The advantages of implementing ideas in a programming language instead of in plain mathematics are that they are type checked and often even executable. In practice, we do not feel constrained by notational restrictions imposed by the use of concrete syntax, although it takes a lot of care to hide unimportant details. On the other hand, it is perhaps too easy to omit essential details when using mathematical notation.

As heavy users of functional languages we felt an ever increasing need to have our own implementation of a Haskell-like language. This would allow us to use the feedback we get from teaching to improve our programming language directly, without being dependent on other implementors who might have different priorities and goals. Understandably Haskell developers are best served by a stable language and thus reluctant to change.

Our home grown compiler should be simple, small, extendible, and written in its own source language. Efficiency is not particularly important. To be competitive with the imperative language implementations our students know and use at home on their PCs (Visual Basic, Visual C++, Visual J++ and Delphi), the implementation should come with a fancy graphical programming environment. A second drive for contriving a Haskell dialect is our belief that in order for functional programming to succeed in the real world, some support for object orientation is a necessary (but not sufficient) condition. As Hughes and Spurd argue [15], Haskell currently lacks the form of incremental reuse that is offered by inheritance in object-oriented languages. Using inheritance you can extend (subclass) a given data type and then redefine only those operations for which the extension is significant while reusing the rest.

There are already several implementations of Haskell-like languages around, most notably the Glasgow [2] and Chalmers [3] Haskell Compilers, Mark Jones's Gofert and Hugs systems [4], Niklas Røjemo's Nearly Haskell Compiler [5], and Clean [6]. So why on earth would anyone want to develop yet another language? The reason is that none of these existing implementations exactly fits our needs. Though one of the goals in the design of GHC was to provide a modular foundation that other researchers can extend and develop, the Glasgow compiler is much too large and complicated to be used.

¹ A sufficient condition would be a killer application in which functional programming is clearly superior. We anticipate that using functional languages, instead of Visual Basic, as glue for COM components could be such a domain.

3 Classes and algebraic data types

For education, Gofert (and Hugs) are small and simple, but they are written in C. The NHC system is written in Haskell, but is optimized for space efficiency. Lastly, the Clean compiler is written in C and optimized for both fast compilation and fast target code. Except for Gofert/Hugs, none of the above implementations has a proper PC/Windows based programming environment.

We recognize that building a complete implementation from scratch is a lot of work, and hard to accomplish with the limited resources we have. Therefore we decided to piggyback on existing infrastructure as much as possible by compiling Mondrian into Haskell. Later we hope to target at Henk [24] as a common intermediate language with GHC. At this moment Mondrian is in its embryonal stage, and it might take a long time before it is delivered. Even so, the ideas ventilated in Mondrian have already prompted the development of a typed intermediate language Henk [24] and helped to keep Haskell on its toes [23, 20, 21].

Mondrian unifies algebraic types and type classes into a simple, simple-minded, object-oriented class mechanism. Dictionaries that are used in the Haskell implementation of algebraic data types [14, 9, 30] are nothing more than algebraic data types with polymorphic fields. Structures with polymorphic components are completely standard and already supported by several existing Haskell implementations [18, 28]. When class dictionaries are first class values, algebraic data types can be modeled by a root class with a subclass for each alternative. Let's see how this all works in some more detail.

As our running example we use a class `Student` that models students that carry a name and an address.

```
class Student where {name, address :: String}
```

We can use the constructor `Student{...}` to construct instances of the `Student` class (values of type `Student`) by defining the fields of interest between the braces as in the following definition of some arbitrary student:

```
student = Student
  { address = "4711 NW One Way Street"
  ; name = "John Doe"
  }
```

Instances of `Student` can be updated non-destructively. When John Doe moves, we might want to change his address

```
student{address = "1478 SW Osprey Drive"}
```

An update of an object creates a new copy in which the specified fields are replaced by the indicated values.

Besides construction and update we can also do pattern matching on class instances. Function `showStudent` does a pattern match on the constructor `Student{...}` to destruct a student value. It maps an instance of the class `Student` to a string.

²In an object-oriented setting one would define this function as a method of the `Student` class, but here we want to discuss the traditional "pattern matching" view of first class classes